

A TeV Scale Origin for Higgs and Flavour?

Joe Davighi, CERN

UCL particle physics seminar, 22nd November, 2024



Outline of the Talk

1. Introduction: the mysteries of Higgs and Flavour
2. Flavour symmetries: from MFV to U_2
3. Flavour deconstruction: solving the flavour puzzle near the TeV
4. Flavour deconstructing the Composite Higgs: solving flavour + hierarchy problem near the TeV

If you remove the Higgs, the Standard Model is a gauge theory with $x3 g_i = O(1)$.

This Higgs-less SM is completely natural!

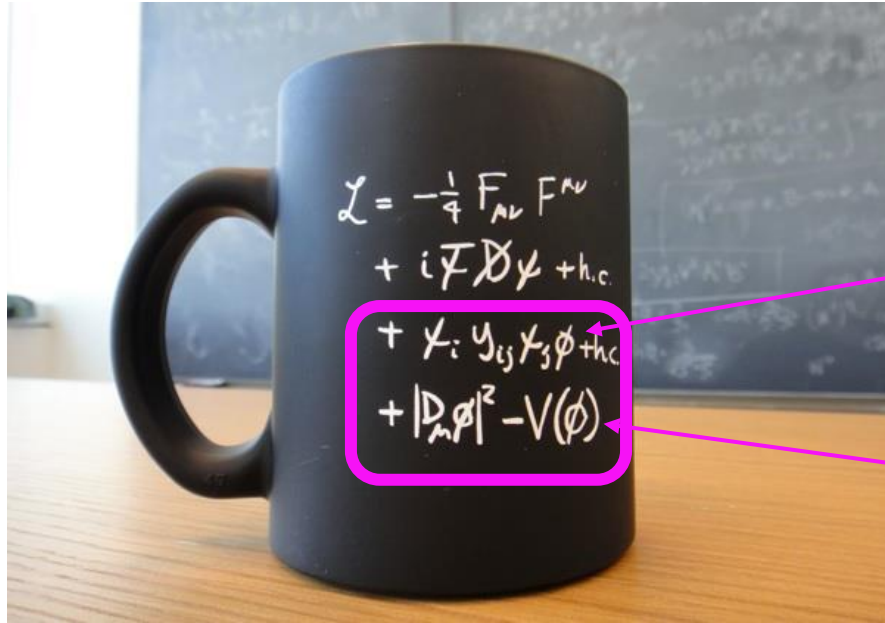
~~Hierarchy problem~~

~~Flavour puzzle~~

~~Strong CP problem~~ [massless quarks]

Higgs = key to BSM, both theoretically & experimentally
(modulo dark sectors)





Flavour puzzle!


Hierarchy problem!

The Hierarchy Problem

*The Higgs has an unnaturally small **mass** parameter:

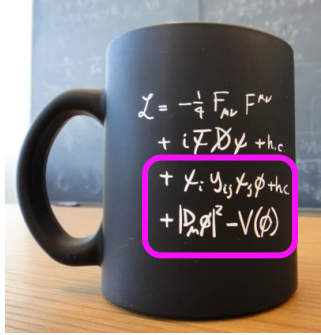
Large hierarchy: $\mu^2 \ll \Lambda_{\text{high scales}}^2$

[Λ could be new particles at GUT scale, flavour scale, PQ scale, neutrino see-saw scale, Planck scale...]

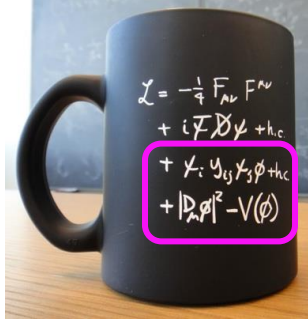


The diagram shows two Higgs bosons (H) connected by dashed lines representing gluon (g) interactions. A loop of a heavy particle X is shown in the center, enclosed in a dashed circle. The particle X is labeled "Heavy particle X".

$$\Rightarrow \delta M_h^2 \Big|_{\text{from } X} = \frac{\mathcal{O}(1)}{16\pi^2} g^2 M_X^2$$



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Two well-understood solutions: **Higgs' compositeness** or **supersymmetry** as low scale as possible

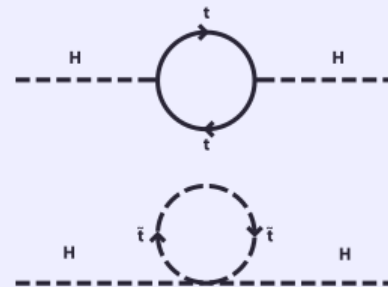
Composite Higgs

- Loops cut off by composite resonances
- To get $m_h \ll m_{\text{res}}$, need Higgs to be pseudo-Goldstone bosons (\sim QCD pions)
- Explicit breaking by top Yukawa and EW gauging generates m_h^2 at 1-loop

$$\delta m_h^2 \sim \frac{1}{16\pi^2} (\#n_c y_t^2 M_T^2 - \#g_1^2 M_\rho^2)$$

Supersymmetry

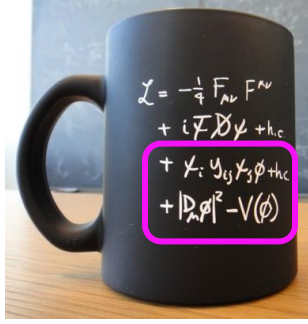
Inclusion of superpartner loops removes quadratic sensitivity to UV cut-off due to bose vs fermi cancellation



$$\Rightarrow \delta m_h^2 \approx \frac{3}{2\pi^2} \frac{m_t^2}{v^2} M_T^2 \log \frac{\Lambda^2}{M_T^2}$$

$$\text{vs } \delta m_h^2 \approx \frac{3}{2\pi^2} \frac{m_t^2}{v^2} \Lambda^2 \text{ for top alone}$$

The Hierarchy Problem



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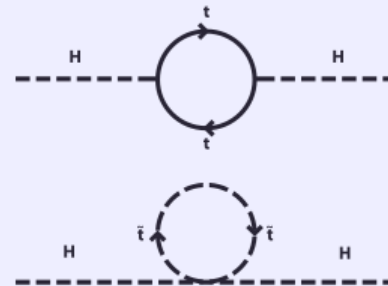
Two well-understood solutions:

Most natural (i.e. least tuned) expectation:
 New particle masses $M_* \lesssim (\text{loop factor})^{-1/2} m_h \sim \text{few TeV}$

- Loops cut off by composite resonances
- To get $m_h \ll m_{\text{res}}$, need Higgs to be pseudo-Goldstone bosons (\sim QCD pions)
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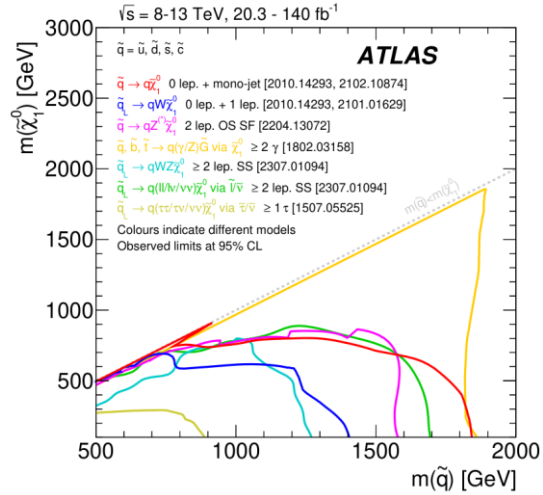
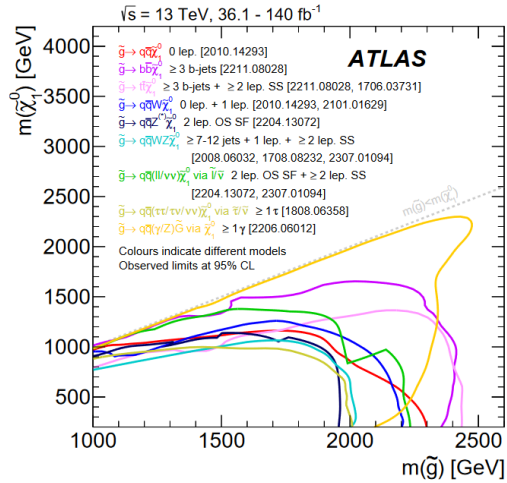


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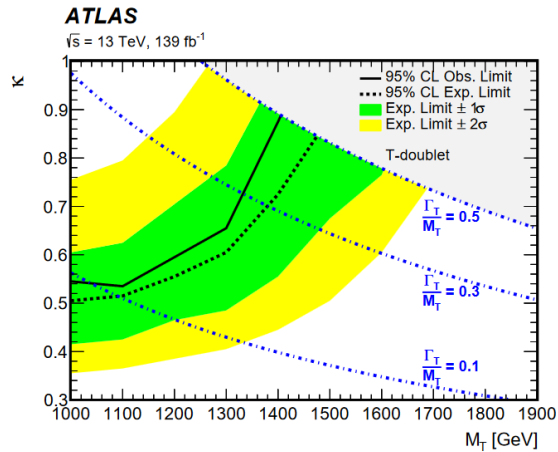
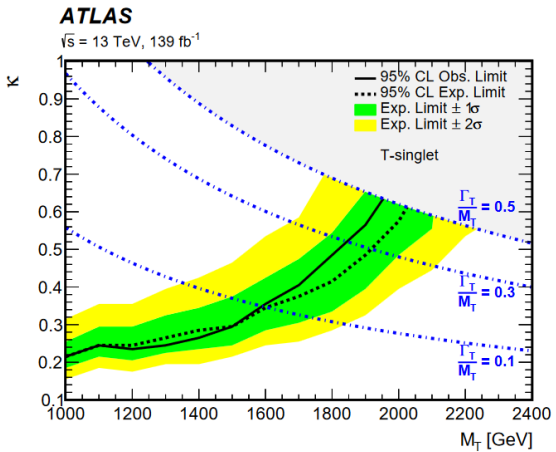
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We are now probing natural M_* directly at the LHC

Few TeV limits on SUSY particles, top partners!



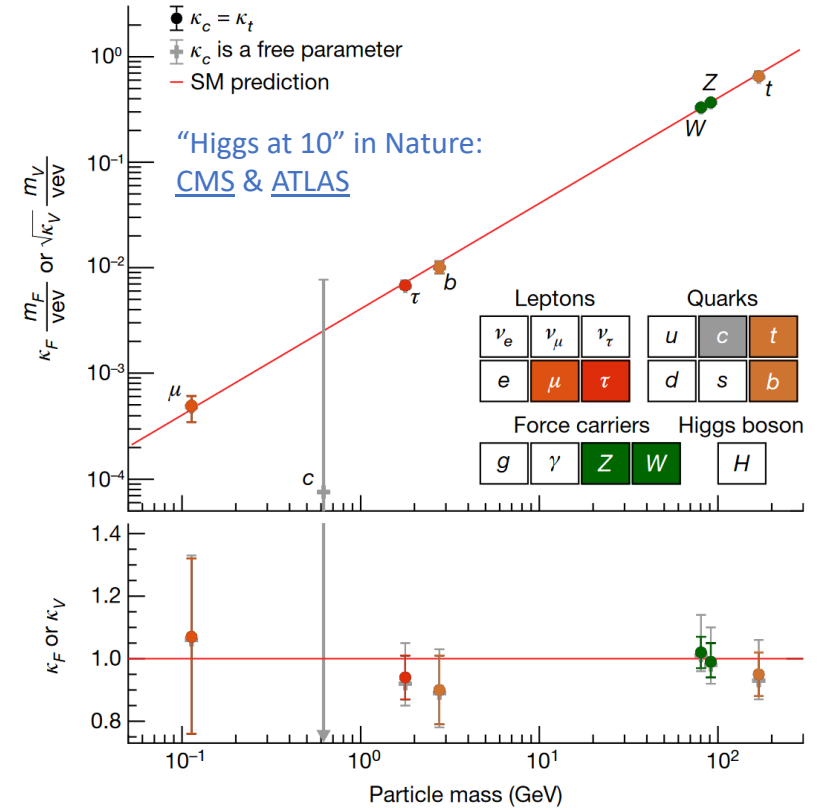
ATLAS, [2403.02455](https://arxiv.org/abs/2403.02455)



ATLAS, [2307.07584](https://arxiv.org/abs/2307.07584)

$$\Rightarrow \frac{\delta m_h^2}{m_h^2} \sim \left(\frac{M_T}{500 \text{ GeV}} \right)^2$$

+ No sign of compositeness in Higgs couplings!
 HWW, HZZ at LHC agree with SM to 3%



$\Rightarrow \frac{v^2}{f^2} \lesssim 5\%$
 where f is compositeness scale

The Hierarchy Problem(s)

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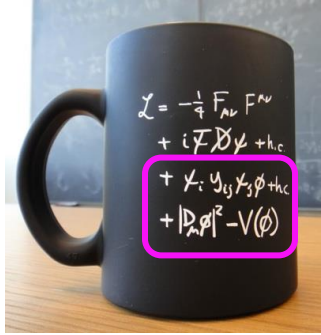
Large hierarchy: $\mu^2 \ll \Lambda_{\text{high scales}}^2 \Rightarrow$ **compositeness** or **SUSY** as low scale as possible

Little hierarchy: $\mu^2 \ll \Lambda_{\text{SM}}^2 \sim \text{TeV}^2 \Rightarrow$ accept it! or try even clever-er model-building

E.g. "Gegenbauer Goldstones"

Durieux, McCullough, Salvioni [2110.06941](#), [2202.01228](#)

Will return to the little hierarchy at the end of the talk...

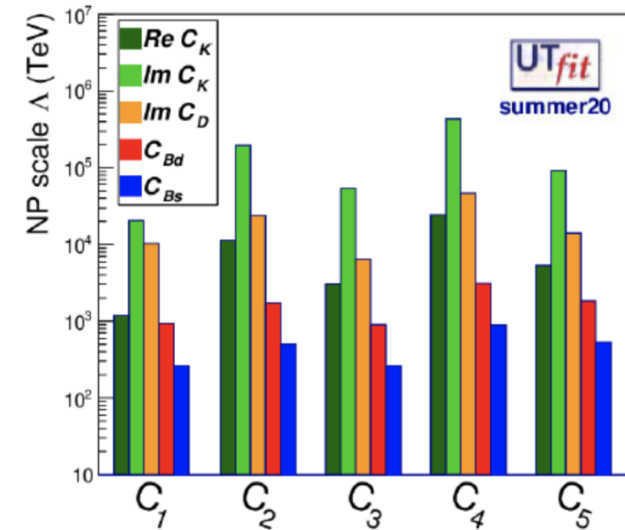
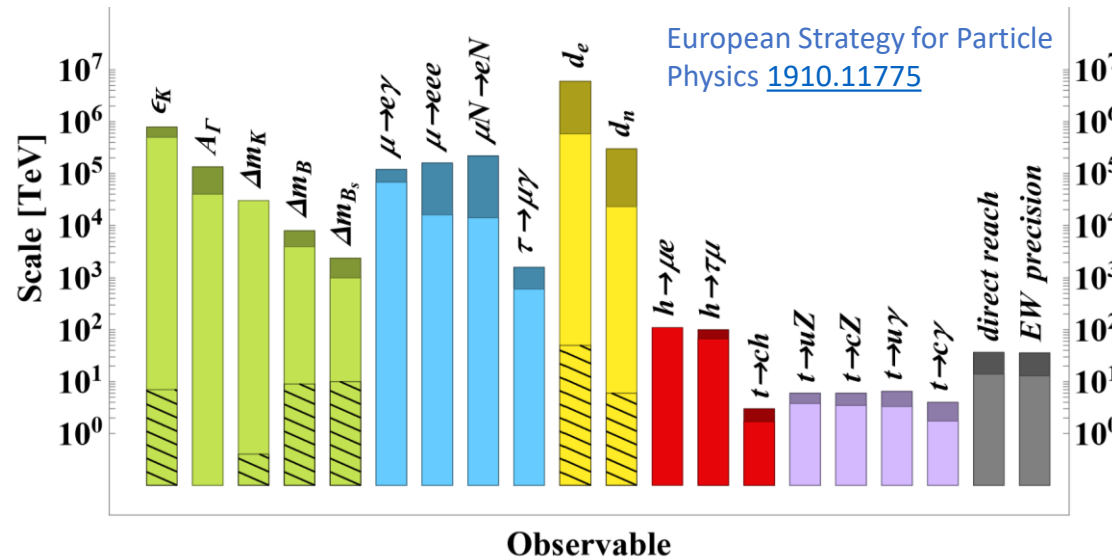


When trying to solve the (large or little) hierarchy problem, we **cannot** ignore flavour!



The BSM Flavour Puzzle

While the hierarchy problem points to scale $M_* \sim \text{TeV}$, flavour points to much higher scales!

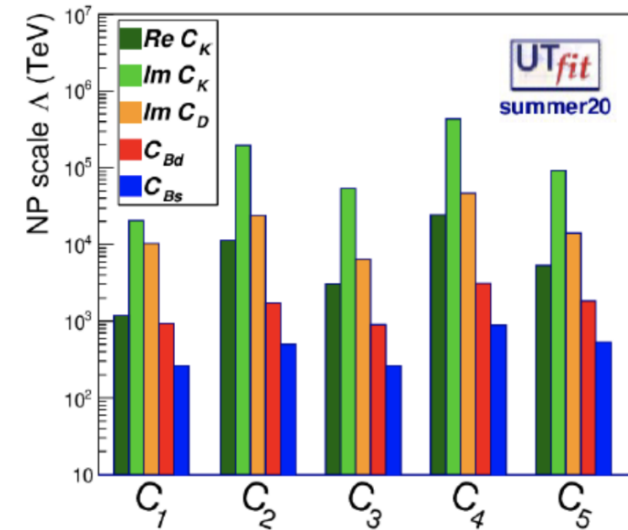
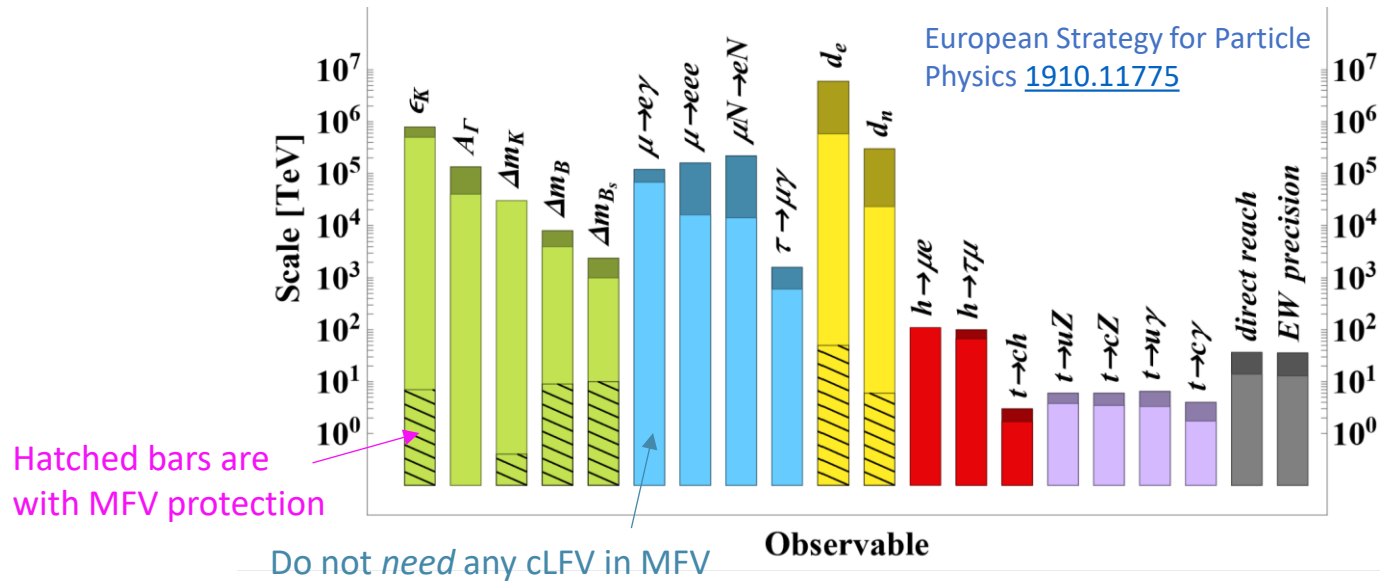


E.g. kaon mixing: $L \supset \frac{e^{i\alpha}(\bar{d}s)^2}{\Lambda_{sd}^2} \Rightarrow \Lambda_{sd} \gtrsim 10^{5\div 6} \text{ TeV}$

Therefore *any* solution to hierarchy problem **needs** non-trivial **flavour structure**

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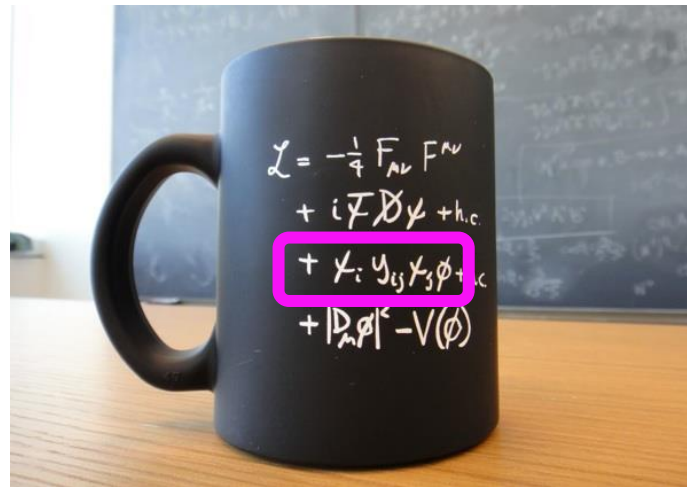
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Example = **Minimal Flavour Violation**: BSM couplings $C_{ij} \sim \delta_{ij} + \dots$, with ... built from SM Yukawas

Kaon mixing with MFV: $\frac{1}{\Lambda_{sd}^2} \sim y_t^4 (V_{31} V_{32}^*)^2 \frac{1}{\Lambda_{\text{NP}}^2} \sim \left(\frac{10^{-5}}{\Lambda_{\text{NP}}}\right)^2$ is sufficient flavour protection!

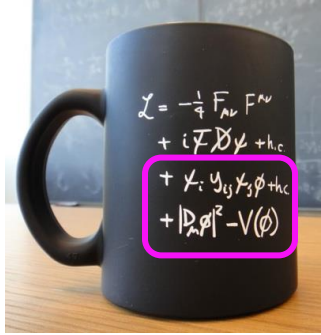
Flavour is already a rich source of mysteries within the SM



The SM Flavour Puzzle(s)

Fermion sector of SM contains many mysteries:

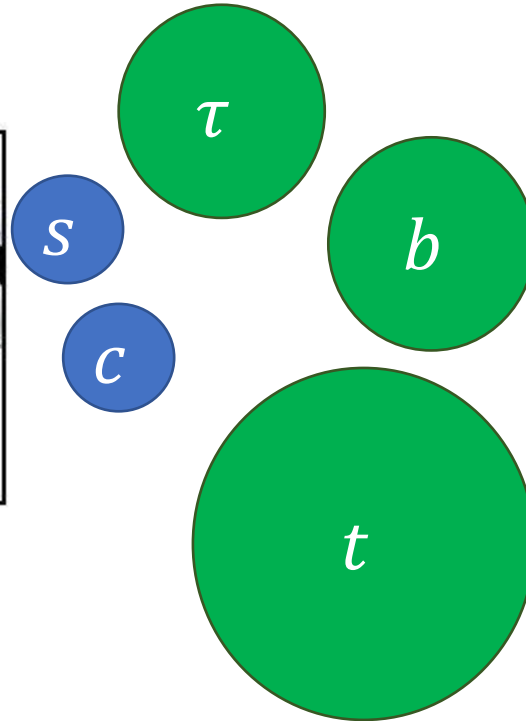
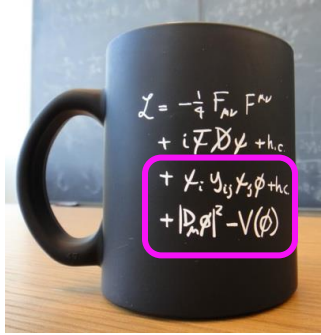
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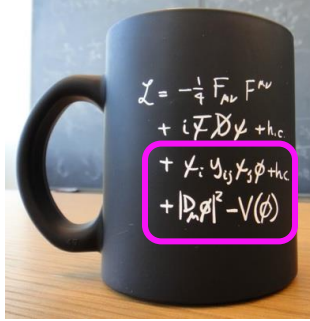
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1. Why those (chiral) representations / hypercharges?
2. Why 3 generations?
3. Why huge (technically natural) hierarchies in SM Yukawa couplings $y_{ij}^f \bar{f}_{L,i} H f_{R,j}$?

Masses: $1 \approx y_t \gg y_c \gg y_u \sim 10^{-5}, y_e \sim 10^{-6}$

Mixings: $V_{us} \gg V_{cb} \gg V_{ub}$



Most of the Higgs' couplings in the SM are generating **flavour!** Higgs is the origin also of the flavour puzzle

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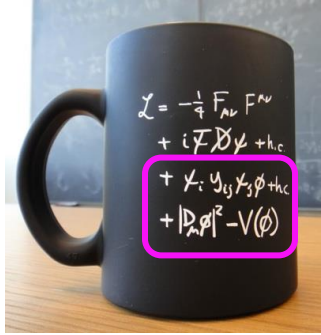
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Does puzzle (3) have a dynamical explanation?

- y_{ij}^f are marginal (dimension-4) interactions: do not clearly point to a particular scale for NP explanation, unlike μ^2
- BUT since Higgs is origin of hierarchy problem & flavour puzzle: **maybe they have a joint solution near TeV?**



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2. From MFV to U2

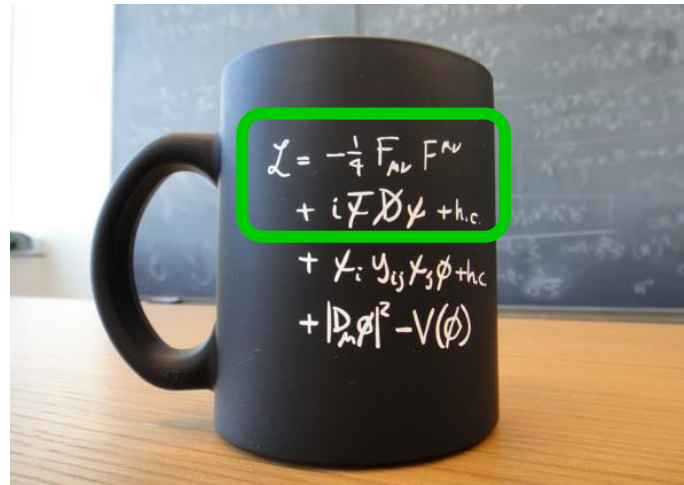


The case for flavour *non*-universal New Physics

U2: Global Symmetries of the SM

SM without Yukawas has a large $U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_l \times U(3)_e$ global symmetry

[SM gauge interactions are flavour-universal]



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[SM gauge interactions are flavour-universal]

SM Yukawas y_{ij}^f are a weak breaking of this $U(3)^5 \rightarrow U(1)_B \times \prod_{i=1}^3 U(1)_{L_i}$; but only y_{33}^u is order-1

$$y_{ij}^u \approx \begin{pmatrix} & & \\ & < 0.01 & 0.04 \\ & & 1 \end{pmatrix} \leftarrow \text{Top Yukawa}$$

Leaves unbroken an approximate $U(2)_q \times U(2)_u$ flavour symmetry, with $(q_1, q_2) \sim \mathbf{2}, q_3 \sim \mathbf{1}$ of $U(2)_q$ etc

Leading “spurions” needed to populate y_{ij}^f are:

- $V_q \sim \mathbf{2}$ of $U(2)_q \rightarrow V_{cb} \sim 0.04$
- $\Delta_u \sim (\mathbf{2}, \mathbf{2})$ of $U(2)_q \times U(2)_u \rightarrow y_c/y_t \sim 0.01$

U2: Global Symmetry of New Physics?

We saw that TeV scale NP needs a special flavour structure e.g. MFV

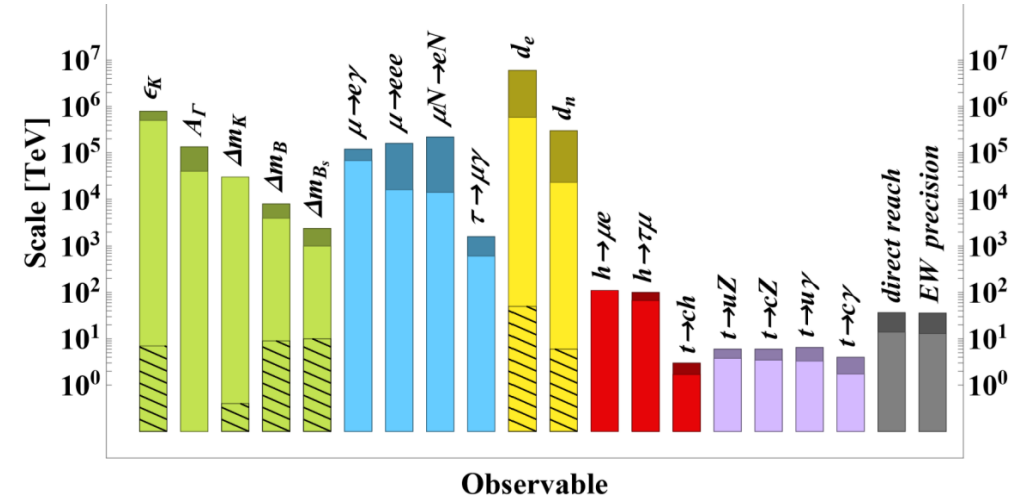
U2 is just as good as MFV for evading flavour bounds

[spurions used to build flavour-violating operators are now V_q and Δ_u etc, rather than y^f themselves as in MFV]

Barbieri et al [1105.2296](#), Isidori, Straub [1202.0464](#), Fuentes-Martin et al, [1909.02519](#)

U2 is a **weaker assumption** on NP than MFV: can decouple 3rd generation from light generations

$$C_{ij} \sim \begin{pmatrix} a & & \\ & a & \\ & & b \end{pmatrix} + \dots$$



MFV:

$(q_1, q_2, q_3) \sim \mathbf{3}$ of $U(3)_q$

Spurions = y^f (most predictive)

U2:

$(q_1, q_2) \sim \mathbf{2}, q_3 \sim \mathbf{1}$ of $U(3)_q$

Spurions = V_q, Δ_u etc

Two big reasons to prefer U2 over MFV

$$C_{ij}^{\text{U2}} \sim \begin{pmatrix} a & & \\ & a & \\ & & b \end{pmatrix} + \dots \quad \text{vs} \quad C_{ij}^{\text{MFV}} \sim \begin{pmatrix} 1 & & \\ & 1 & \\ & & 1 \end{pmatrix} + \dots$$

1. **Theoretical**: same global symmetry as the SM Yukawas \Rightarrow can **explain SM flavour puzzle** at same time!

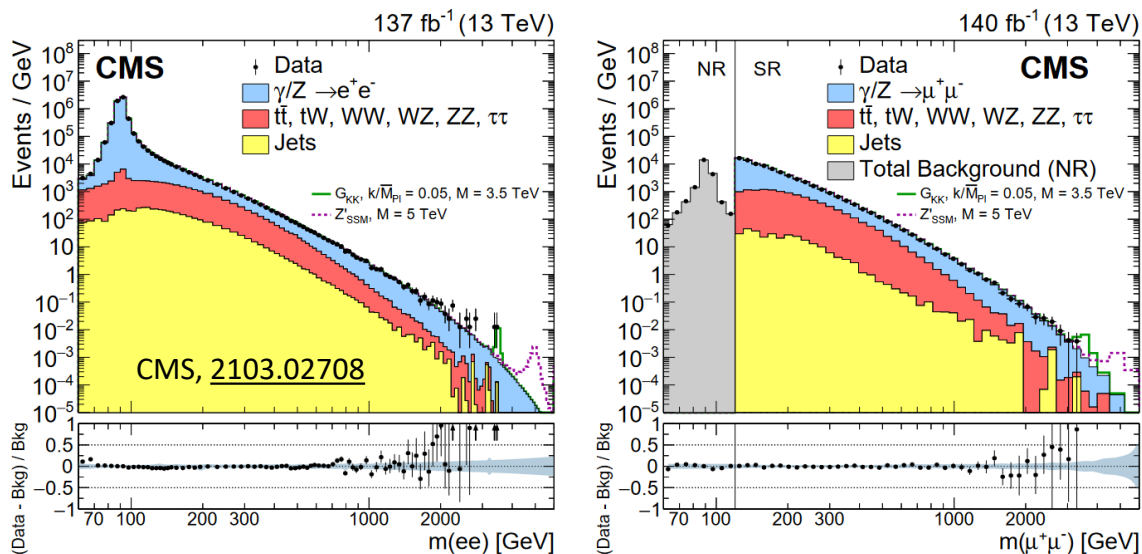
2. **Phenomenological**: weaker collider bounds!

The scale Λ_{NP} can be reduced by taking $a \ll b$, allowing $\Lambda_{U(2)} \sim 1 \text{ TeV}$ vs $\Lambda_{\text{MFV}} \sim 10 \text{ TeV}$;

in the LHC era this allows for **more natural models** than with MFV

Lowering Λ_{NP} with U2

Exhibit A: High- p_T Drell-Yan tails $pp \rightarrow ll$

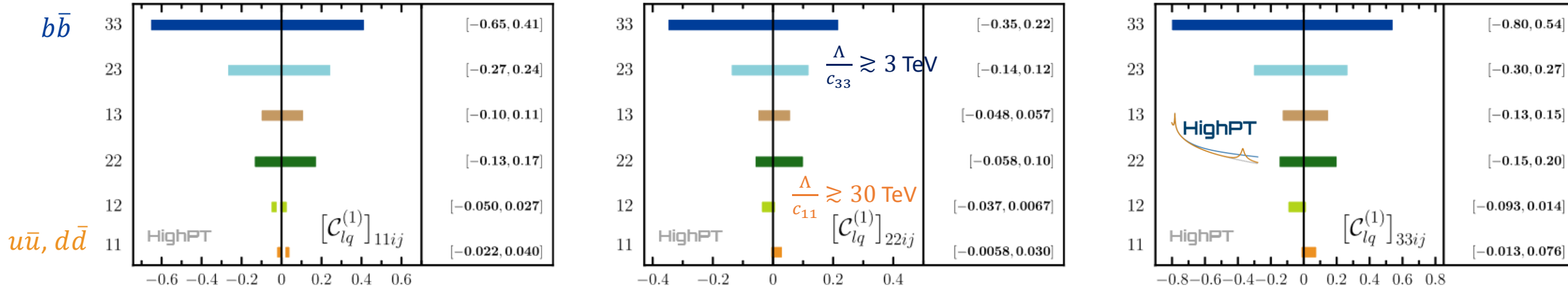


Bounds on dim-6 semi-leptonic operators:

$$L_{SMEFT} \supset \frac{C_{lq}^{(1)}}{1 \text{ TeV}^2} \bar{l} \gamma^\mu l \bar{q} \gamma_\mu q$$

Allwicher, Faroughy, Jaffredo, Sumensari, Wilsch, [2207.10714](#)

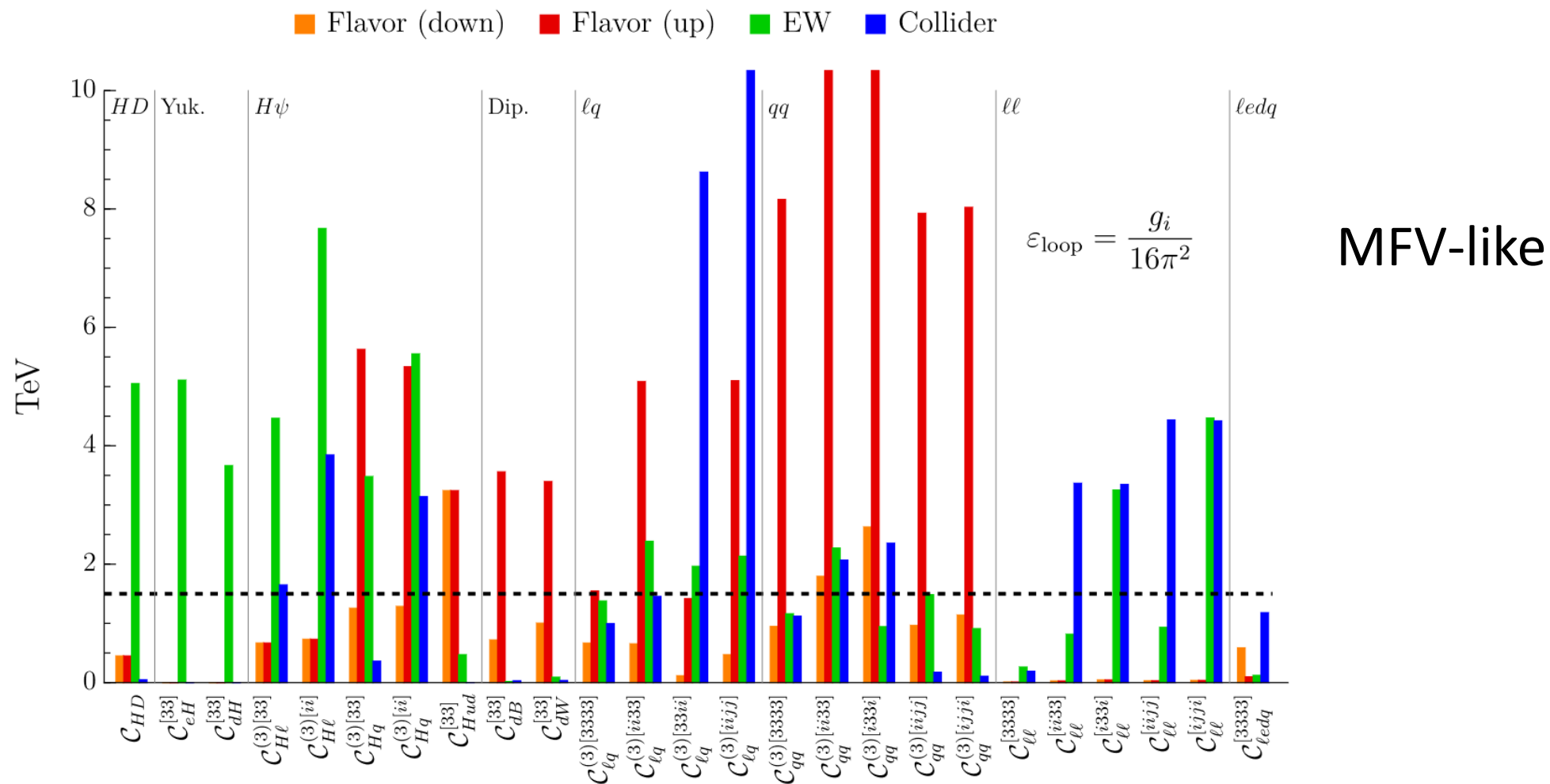
Allwicher, Faroughy, Jaffredo, Sumensari, Wilsch, [2207.10756](#)



Lowering Λ_{NP} with U2

Exhibit B: global lessons from SMEFT likelihoods

Allwicher, Cornella, Isidori, Stefaneke, [2311.00020](#)

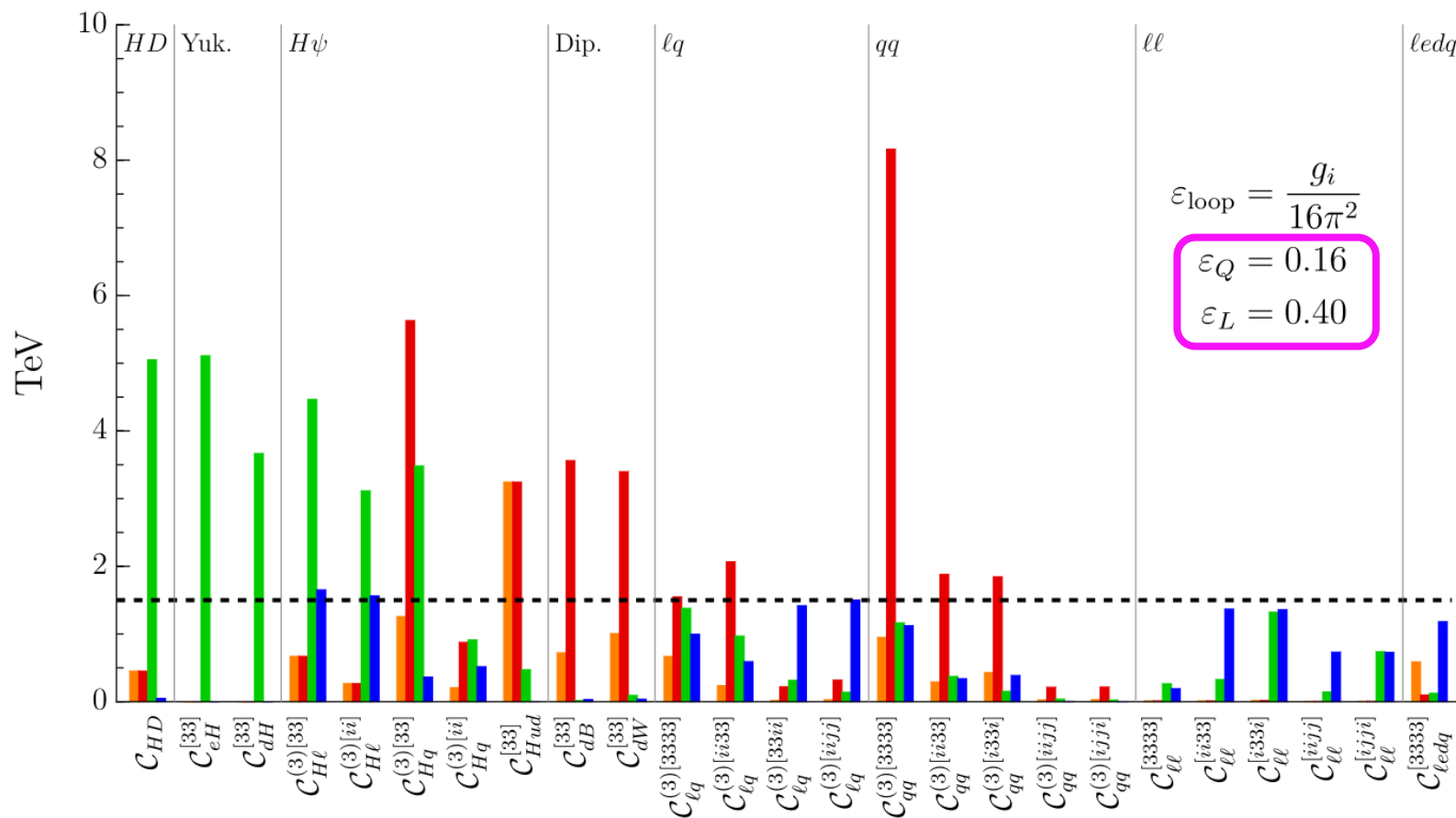


Lowering Λ_{NP} with U2

Exhibit B: global lessons from SMEFT likelihoods

Allwicher, Cornella, Isidori, Stefaneke, [2311.00020](#)

■ Flavor (down)
 ■ Flavor (up)
 ■ EW
 ■ Collider



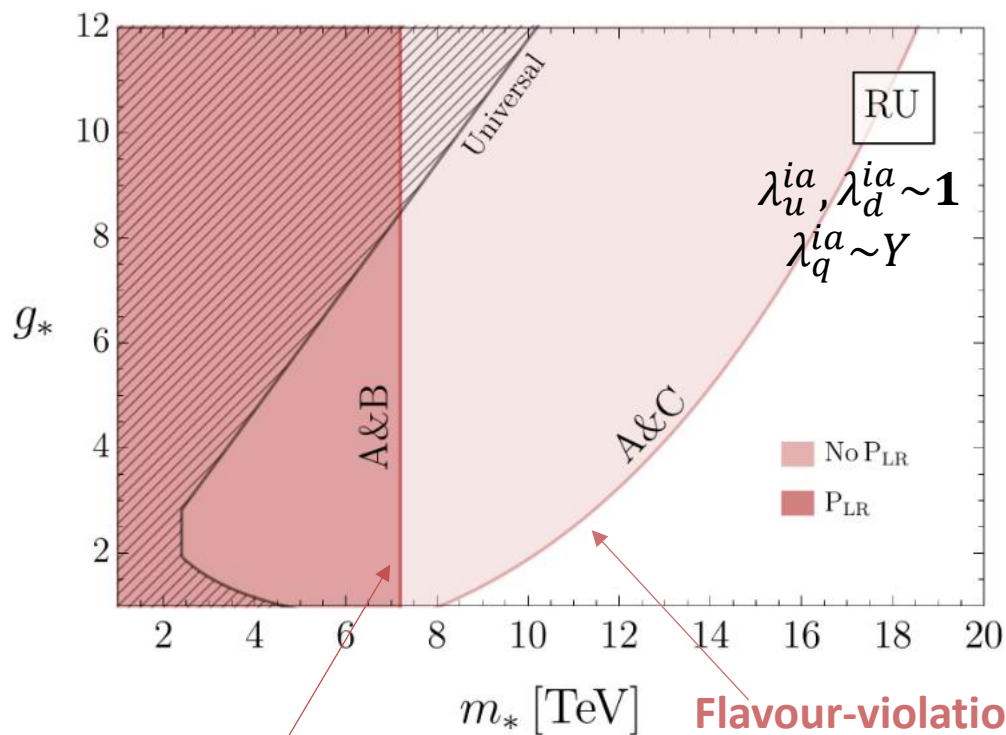
U2-like

Mild suppression of operators with light-generation quarks and leptons

Lowering Λ_{NP} with U2

Exhibit C: composite Higgs solutions to hierarchy problem

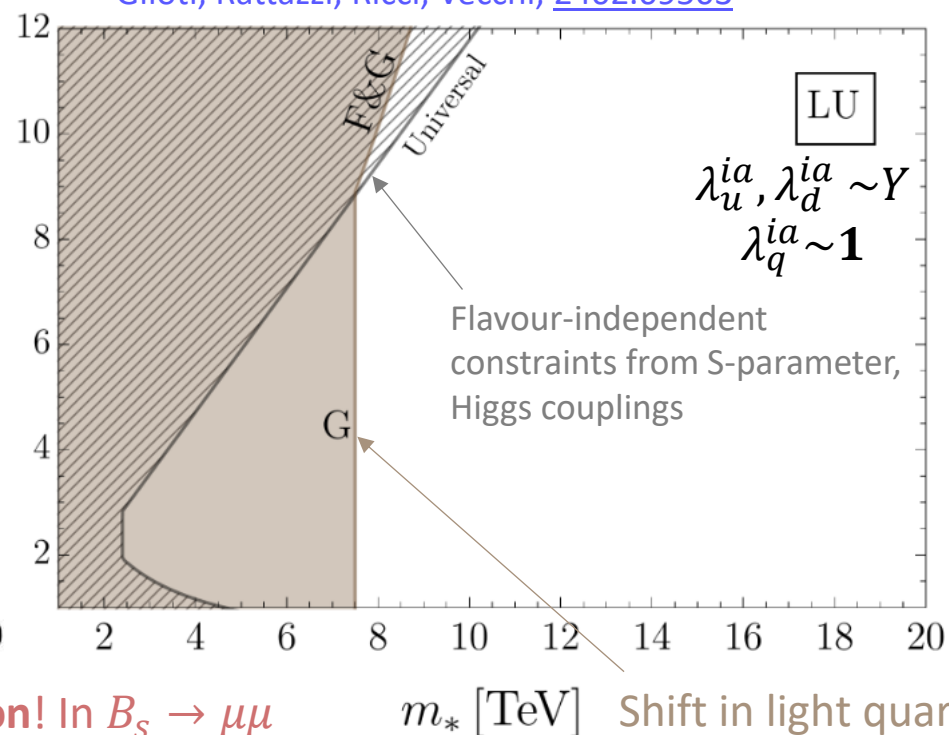
With MFV: $M_* \gtrsim 7 \div 8$ TeV



Di-jet constraints from LHC, driven by light quark couplings

P_{LR} is an extension of custodial by a 'left-right' exchange symmetry
[kills $Zb_L b_L$ correction]

Glioti, Rattazzi, Ricci, Vecchi, [2402.09503](#)



Shift in light quark couplings to W boson

Strongest current bounds are driven by couplings to **light generation fermions OR flavour violation**, not EW constraints

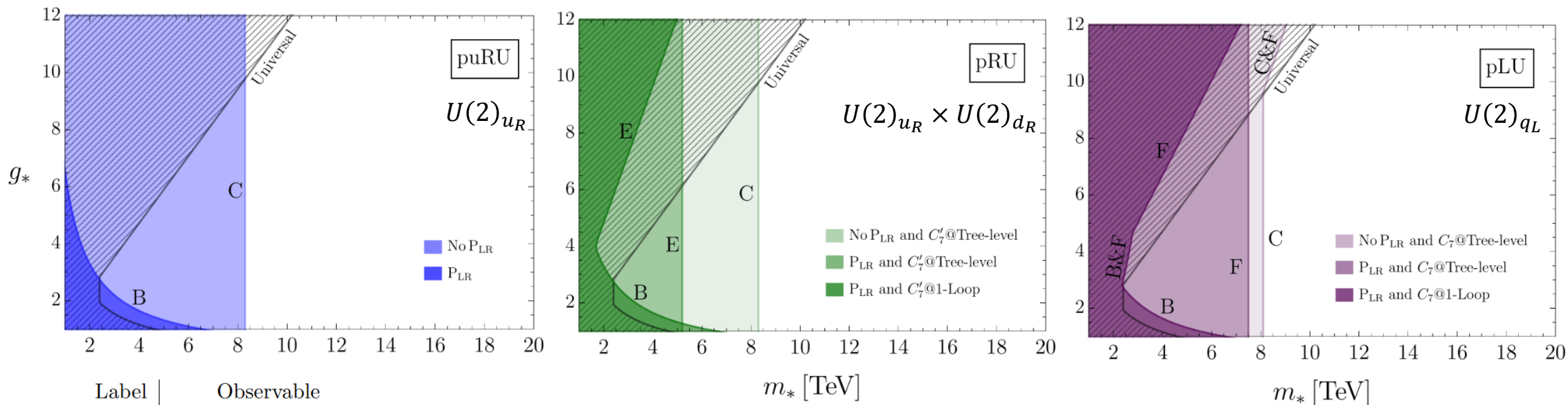
Label	Observable
A	$pp \rightarrow jj$
B	$\Delta F = 2 (B_d)$
C	$B_s \rightarrow \mu^+ \mu^-$
D	nEDM
E	$B^0 \rightarrow K^{*0} e^+ e^- (C_7')$
F	$B \rightarrow X_s \gamma (C_7)$
G	W-coupling

Lowering Λ_{NP} with U2

Exhibit C: composite Higgs solutions to hierarchy problem

With U2: $M_* \gtrsim 1 \div 2$ TeV

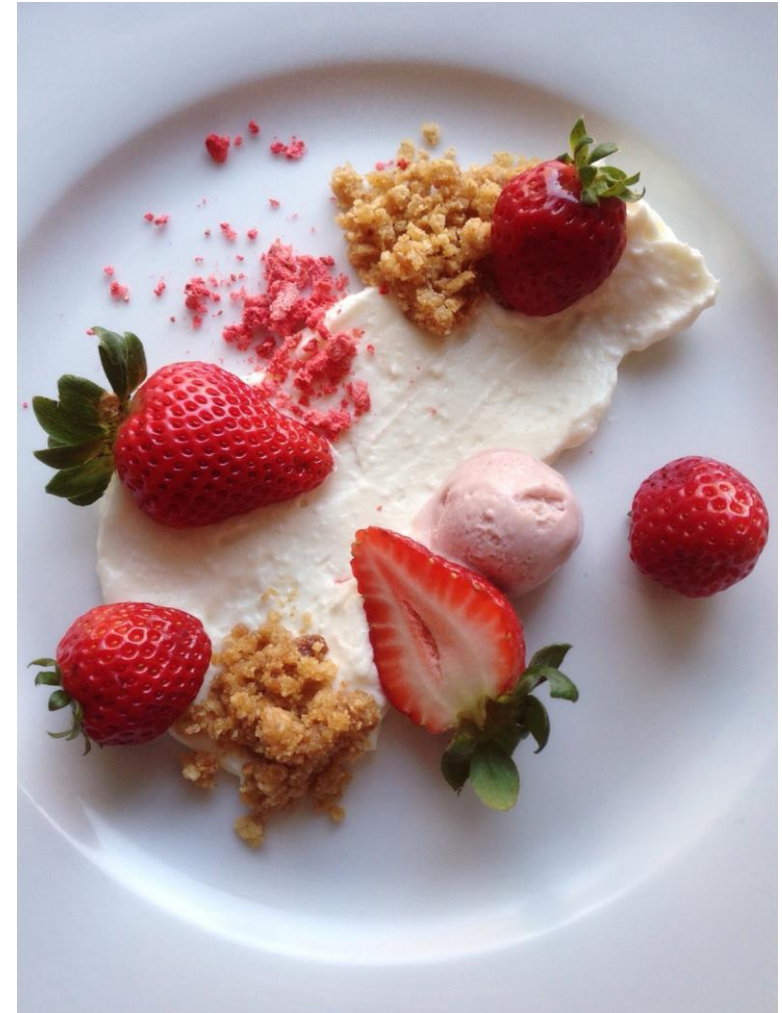
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G	W-coupling

Going from MFV to U(2), we decouple the strong LHC constraints: dominant bounds now heavy-to-light quark flavour-violation + universal EW constraints

3. On the Origin of U2: Flavour Deconstruction



So far we have considered the phenomenological consequences of $U(2)^n$ as an imposed global symmetry of NP. What might be the origin of this $U(2)^n$?

General hypothesis:

- The $U(2)$ s manifest in Yukawas and NP couplings have common dynamical origin:
- = accidental symmetries from a **flavour non-universal [3 vs 1+2] gauge symmetry**, broken \sim TeV

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But what symmetry to gauge? There are many options...

Flavour non-universal gauge interactions

Horizontal Approach: $G = G_{\text{SM}} \times G_{\text{hor}} \rightarrow G_{\text{SM}}$

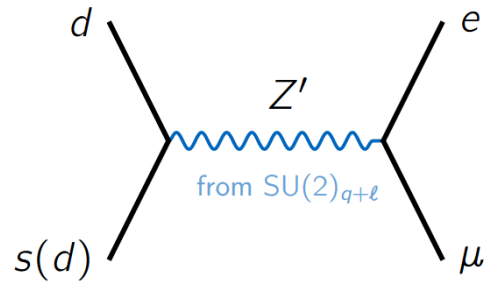
Froggatt, Nielsen, [Nucl Phys B \(1979\)](#)

Gauge some $H \subset U(2)^n$ directly, and break to nothing

Gives a bunch of Z' bosons that can be decoupled from the Higgs (can take $g \ll 1$)

But they are flavour-violating and so **high scale**

- Bounds e.g. from LFV decay $K_L \rightarrow \mu^\pm e^\mp \Rightarrow \frac{M}{g} \gtrsim 10^{2\div 3} \text{ TeV}$



Recent examples:

Allanach, Davighi, [1809.01158](#); [1905.10327](#)

Darmé, Deandrea, Mahmoudi, [2307.09595](#)

Greljo, Thomsen, [2309.11547](#)

Antusch, Greljo, Stefaneck, Thomsen, [2311.09288](#)

Greljo, Thomsen, Tiblom, [2406.02687](#)

Flavour non-universality, non-horizontally

Deconstruction Approach: $G_{12} \times G_{3+H} \rightarrow G_{SM}$

Li, Ma, [1981](#), ...
 Arkani-Hamed, Cohen, Georgi [hep-th/0104005](#) ...
 Craig, Green, Katz [1103.3708](#) ...
 Bordone, Cornella, Fuentes-Martin, Isidori, [1712.01368](#) ...

Multi-scale breaking pattern can explain full Yukawa structure:

$$G_1 \times G_2 \times G_{3+H} \rightarrow G_{12} \times G_{3+H} \quad \text{by } \langle \phi_{12} \rangle \sim 100(0\dots) \text{ TeV}$$

$$\rightarrow G_{SM} \quad \text{by } \langle \phi_{23} \rangle \sim 1(0\dots) \text{ TeV}$$

where e.g. $\phi_{12} \sim (\square, \square)$ of $G_1 \times G_2$

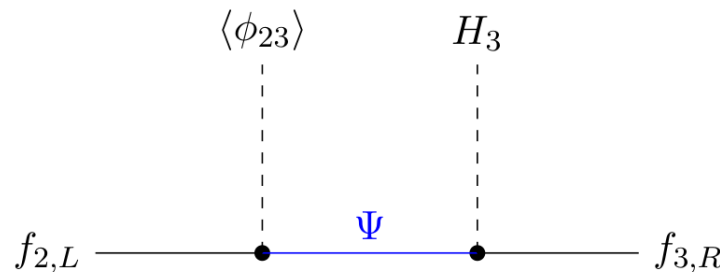
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How it works:

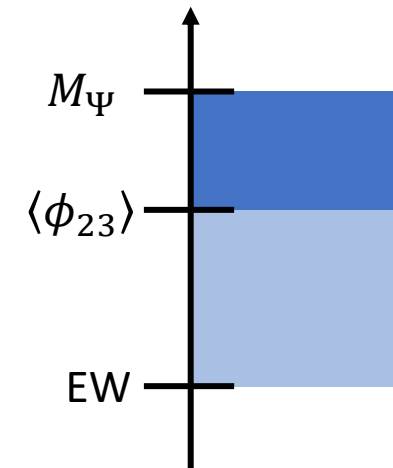
To connect 3rd family / Higgs to 2nd family, need ϕ_{23} insertion $\Rightarrow \epsilon_{23} := \frac{v_{23}}{\Lambda_{23}}$ suppression

To connect 3rd family / Higgs to 1st family, $\phi_{12}\phi_{23}$ insertion $\Rightarrow \frac{v_{12}}{\Lambda_{12}} \frac{v_{23}}{\Lambda_{23}}$ suppression

Example UV:



$$y_{23} \sim \frac{v_{23}}{M_\Psi} = \epsilon_{23}$$



Flavour non-universality, non-horizontally

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$$\begin{array}{llll}
 G_1 \times G_2 \times G_{3+H} & \rightarrow G_{12} \times G_{3+H} & \text{by } \langle \phi_{12} \rangle \sim 100(0\dots) \text{ TeV} & \text{where e.g. } \phi_{12} \sim (\square, \square) \text{ of } G_1 \times G_2 \\
 & \rightarrow G_{SM} & \text{by } \langle \phi_{23} \rangle \sim 1(0\dots) \text{ TeV} & \text{where e.g. } \phi_{23} \sim (\square, \square) \text{ of } G_{12} \times G_{3+H}
 \end{array}$$

Much richer phenomenology! SM-charged vectors in adj G , w flavour diagonal BUT non-universal couplings

$$C_{ij} \sim g_{SM} \begin{pmatrix} g_{12}/g_3 & & \\ & g_{12}/g_3 & \\ & & g_3/g_{12} \end{pmatrix}, \quad g_{12}, g_3 \geq g_{SM}. \quad \text{Define } \tan\theta = g_3/g_{12}$$

- The $G_{12} \times G_{3+H} \rightarrow G_{SM}$ breaking is viable close to TeV because no flavour violation, and $g_3 \gg g_{1,2}$ U2 limit
- Indeed it *cannot* be decoupled from experiment [$M \rightarrow \infty$] w/o creating hierarchy problem [Davighi, Isidori 2303.01520](#)



$$\delta m_h^2 \sim g^2 M^2 / 16\pi^2$$

Flavour non-universality, non-horizontally

Deconstruction Approach: $G_{12} \times G_{3+H} \rightarrow G_{SM}$

Li, Ma, [1981](#), ...

Arkani-Hamed, Cohen, Georgi [hep-th/0104005](#) ...

Craig, Green, Katz [1103.3708](#) ...

Bordone, Cornella, Fuentes-Martin, Isidori, [1712.01368](#) ...

Multi-scale breaking pattern can explain full Yukawa structure:

$$G_1 \times G_2 \times G_{3+H} \rightarrow G_{12} \times G_{3+H} \quad \text{by } \langle \phi_{12} \rangle \sim 100(0\dots) \text{ TeV}$$

$$\rightarrow G_{SM} \quad \text{by } \langle \phi_{23} \rangle \sim 1(0\dots) \text{ TeV}$$

where e.g. $\phi_{12} \sim (\square, \square)$ of $G_1 \times G_2$

where e.g. $\phi_{23} \sim (\square, \square)$ of $G_{12} \times G_{3+H}$

Theoretical appeal:

1. Charge assignment and anomaly-freeness inherited from SM – no *ad hoc* choices
2. Breaking pattern $G_A \times G_B \rightarrow G_{A+B}$, given scalar condensate ϕ , is **generic** for simple G
 - for any scalar rep $\phi \sim (\mathbf{R}_{12} \neq 1, \mathbf{R}_3 \neq 1)$, you *always* break to the diagonal (ergo flavour-universal) subgroup
 - ... because there is no other non-trivial subgroup embedding, by *Goursat's lemma*
3. Easy to find semi-simple UV completions with deconstruction approach
 - In contrast most $G_{SM} \times U(1)_X$, even anomaly-free, have no semi-simple completion

[Goursat, 1889](#)

[Craig, Garcia-Garcia, Sutherland, 1704.07831](#)

[Davighi, Tooby-Smith, 2206.11271](#)

Aside: Electroweak Flavour Unification

Davighi, Tooby-Smith, [2201.07245](#)
Davighi, [2206.04482](#)

Is there a nice UV origin for flavour deconstruction?

One path is to *reunify* the deconstructed symmetry in the UV

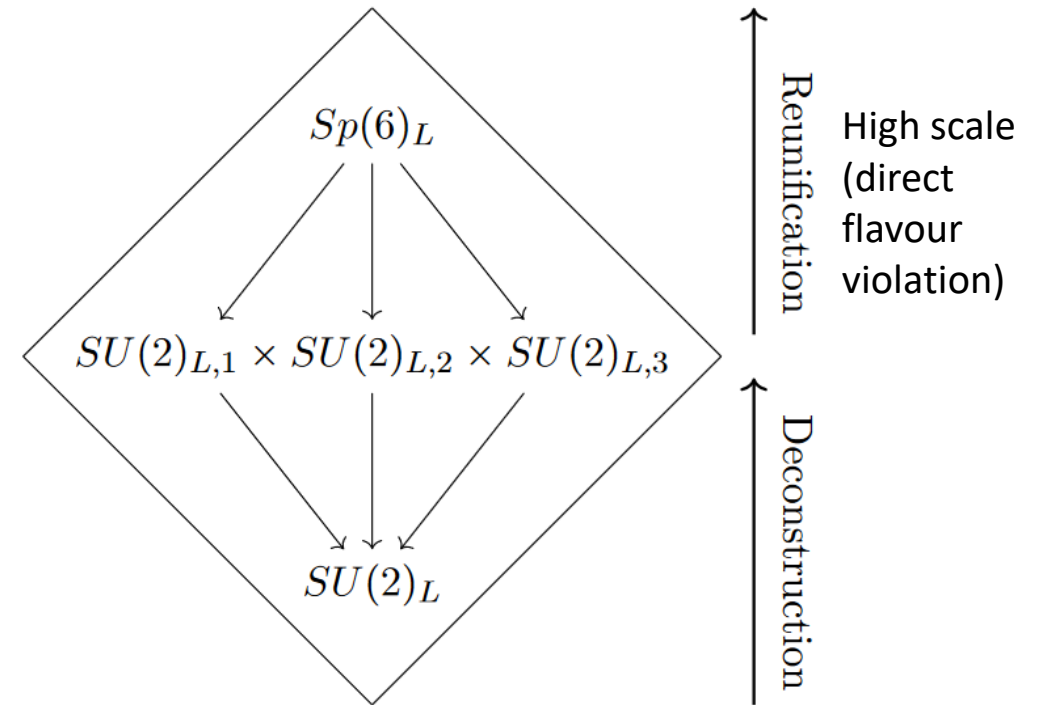
E.g. deconstructed electroweak symmetry $\hookrightarrow Sp(6)_L \times Sp(6)_R$

- Anomaly-free
- New solution to SM flavour puzzle
- Low energy limit (and pheno) is that of flavour deconstruction
- offers a gauge answer to “why 3 generations”?

Reminder:

The Lie group $Sp(6)$ is a subgroup of $SU(6)$:

$$Sp(6) = \{U \in SU(6) | U^T \Omega U = \Omega\}, \text{ where } \Omega = \begin{pmatrix} 0 & I_3 \\ -I_3 & 0 \end{pmatrix}$$



Aside: Electroweak Flavour Unification

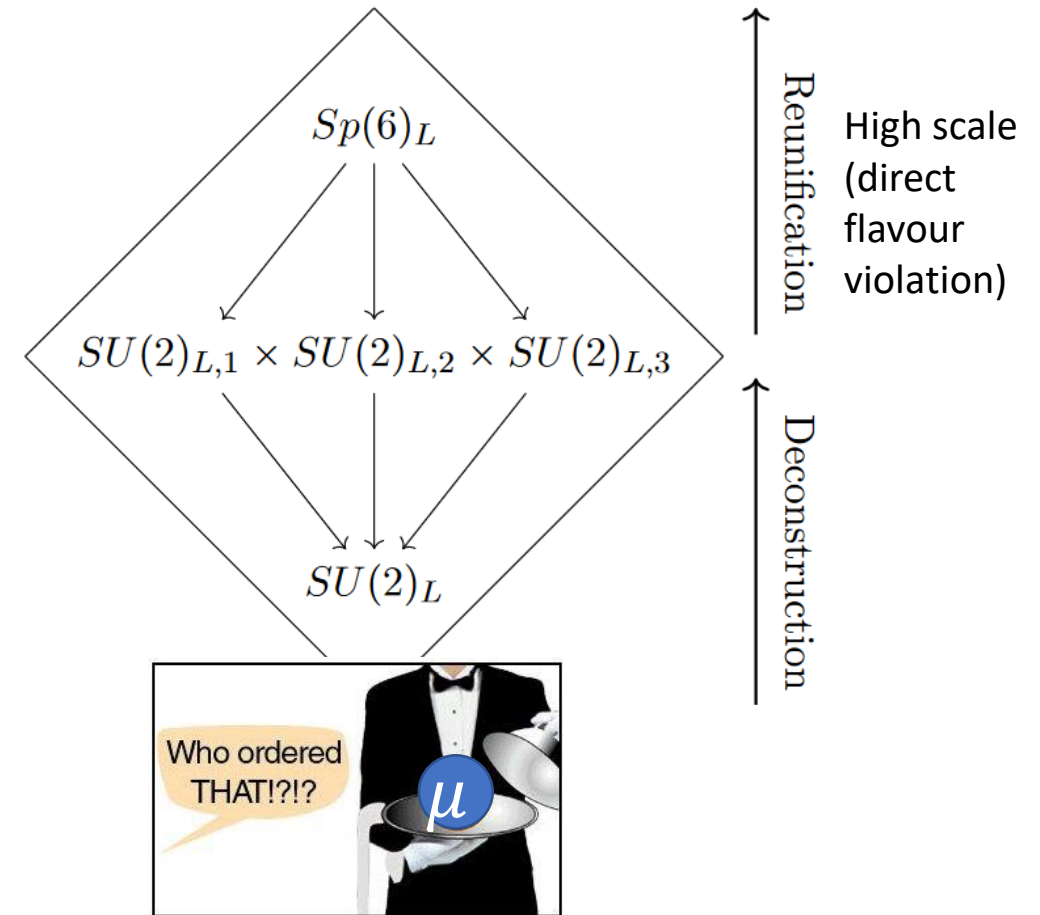
Davighi, Tooby-Smith, [2201.07245](#)
Davighi, [2206.04482](#)

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We arrived at this theory from a different motivation: unification!

If we want to unify all fermions, the only options are EWFU or “colour flavour unification” via $SU(12)$ - but this “anti-solves” the flavour puzzle by setting $y_u = y_c = y_t$ etc at LO

See the classification of all embeddings of 3-flavour SM gauge algebra: Allanach, Gripiaios, Tooby-Smith, [2104.14555](#)

Back to flavour deconstruction

Which SM force should we deconstruct?
And what is the phenomenology?



Survey of Flavour Deconstruction models

Davighi, Isidori [2303.01520](#)

	Deconstructed force	$SU(3)$	$SU(2)_L$	$SU(2)_R$	$U(1)_Y$	$U(1)_{B-L}$
Flavour	$ V_{cb} \ll 1$	✓	✓	×	✓	✓
	$y_i \ll y_3$	×	✓	✓	✓	×
EW	Natural upper limit of $ \tan \theta M$ EWPOs order	90 TeV 1-loop	20 TeV Tree	40 TeV Tree	40 TeV Tree	500 TeV 1-loop

$$Y \sim \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} & & \\ & & \\ \times & \times & \times \end{pmatrix} \quad \begin{pmatrix} & \times & \\ & \times & \\ & \times & \end{pmatrix} \quad \begin{pmatrix} & & \\ & & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix}$$

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	$y_i \ll y_3$	×	✓	✓	✓	×
EW	Natural upper limit of EWPOs order	90 TeV 1-loop	20 TeV Tree	40 TeV Tree	40 TeV Tree	500 TeV 1-loop

“EWPO”s:

	Observable	Definition
Z-pole	Γ_Z	$\sum_f \Gamma(Z \rightarrow f\bar{f})$
	σ_{had}	$\frac{12\pi}{m_Z} \frac{\Gamma(Z \rightarrow e^+e^-)\Gamma(Z \rightarrow q\bar{q})}{\Gamma_Z^2}$
	$R_f (f = e, \mu, \tau, c, b)$	$\frac{\Gamma(Z \rightarrow f\bar{f})}{\sum_q \Gamma(Z \rightarrow q\bar{q})}$
	$A_f (f = e, \mu, \tau, s, c, b)$	$\frac{\Gamma(Z \rightarrow f_L\bar{f}_L) - \Gamma(Z \rightarrow f_R\bar{f}_R)}{\Gamma(Z \rightarrow f\bar{f})}$
	$A_{\text{FB}}^{0,\ell} (\ell = e, \mu, \tau)$	$\frac{3}{4} A_e A_\ell$
	$A_q^{\text{FB}} (q = c, b)$	$\frac{3}{4} A_e A_q$
	R_{uc}	$\frac{\Gamma(Z \rightarrow u\bar{u}) + \Gamma(Z \rightarrow c\bar{c})}{2 \sum_q \Gamma(Z \rightarrow q\bar{q})}$
W-pole	m_W	
	Γ_W	$\sum_{f_1, f_2} \Gamma(W \rightarrow f_1 f_2)$
	$\text{Br}(W \rightarrow \ell\nu) (\ell = e, \mu, \tau)$	
	R_{Wc}	$\frac{\Gamma(W \rightarrow cs)}{\Gamma(W \rightarrow ud) + \Gamma(W \rightarrow cs)}$

$$Y \sim \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} & & \\ \times & \times & \times \end{pmatrix} \quad \begin{pmatrix} & \times & \\ & \times & \\ & \times & \end{pmatrix} \quad \begin{pmatrix} & & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix}$$

LEP-1 and SLC

LEP-2, Tevatron, and LHC

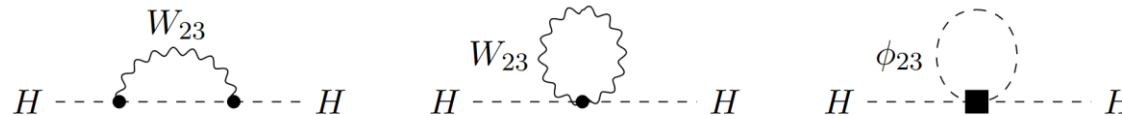
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Flavour	$ V_{cb} \ll 1$ $y_i \ll y_3$	✓ ✗	✓ ✓	✗ ✓	✓ ✓	✓ ✗
EW	Natural upper limit of $ \tan \theta M$ EWPOs order	90 TeV 1-loop	20 TeV Tree	40 TeV Tree	40 TeV Tree	500 TeV 1-loop

$$Y \sim \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} & & \\ \times & \times & \times \end{pmatrix} \quad \begin{pmatrix} & \times & \\ & \times & \\ & \times & \end{pmatrix} \quad \begin{pmatrix} & & \\ & & \times \end{pmatrix} \quad \begin{pmatrix} \times & \times & \\ \times & \times & \\ & & \times \end{pmatrix}$$

“Finite naturalness” limits on M_X from requiring the finite part of $\delta m_h^2 \lesssim 1 \text{ TeV}^2$



General Lesson

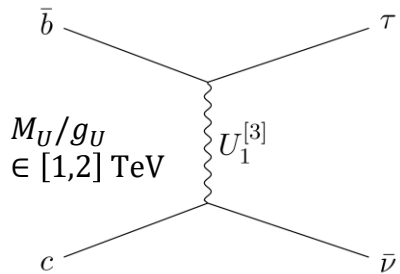
- Need to deconstruct part of the EW symmetry to explain the flavour puzzle (because Higgs is colourless)
- Automatically implies 1-loop δm_h^2 and tree-level δ EWPOs

Survey of Flavour Deconstruction models

Davighi, Isidori [2303.01520](#)

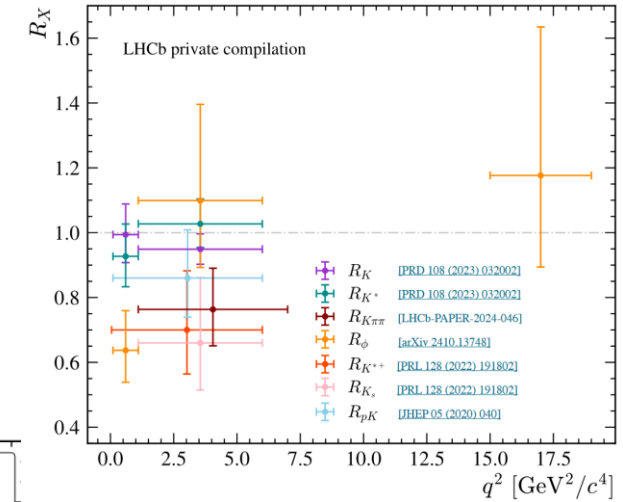
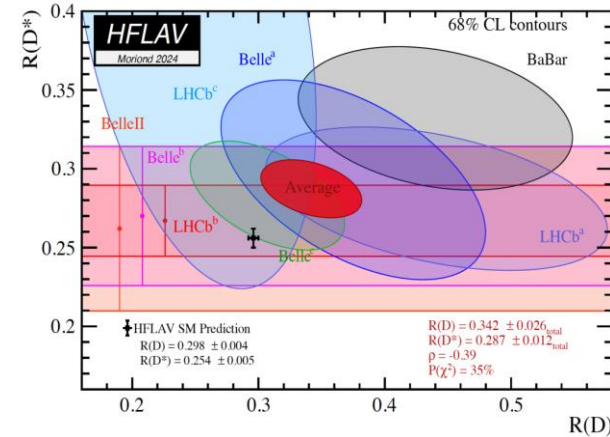
	Deconstructed force	$SU(3)$	$SU(2)_L$	$SU(2)_R$	$U(1)_Y$	$U(1)_{B-L}$
Flavour	$ V_{cb} \ll 1$ $y_i \ll y_3$	✓ ✗	✓ ✓	✗ ✓	✓ ✓	✓ ✗
EW	Natural upper limit of $ \tan \theta M$ EWPOs order	90 TeV 1-loop	20 TeV Tree	40 TeV Tree	40 TeV Tree	500 TeV 1-loop

Aside: If we enlarge $SU(3)^{[3]} \rightarrow SU(4)^{[3]}$, can also explain $b \rightarrow c\tau\nu$ anomalies in $R_{D^{(*)}}$ & $bs\mu\mu$ via '4-3-2-1' models

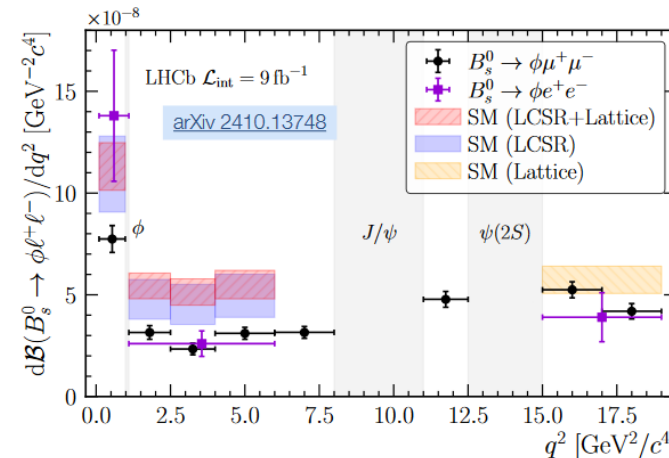


Buttazzo, Greljo, Isidori, Marzocca, [1706.07808](#); Di Luzio, Greljo, Nardecchia, [1708.08450](#); Bordone, Cornella, Fuentes-Martin, Isidori, [1712.01368](#); Greljo, Stefanek, [1802.04274](#); Di Luzio, Fuentes-Martin, Greljo, Nardecchia, Renner, [1808.00942](#); Fuentes-Martin, Stangl, [2004.11376](#) ...

Experimental hints for deconstruction near TeV?



[LHCb Implications 2024](#)



Phenomenology of EW Flavour Deconstruction

Deconstructing $SU(2)_L$ or $U(1)_Y$ gives a 2-parameter model: M_X and $\tan \theta = g_3/g_{12}$

Important SMEFT operators:

$DU(1)_Y$: Davighi, Stefaneke [2305.16280](#)

$DSU(2)_L$: Davighi, Gosnay, Miller, Renner [2312.13346](#)

	Flavour (mixing, $bs\mu\mu$)	LHC Drell-Yan $pp \rightarrow ll (lv)$	Electroweak Precision
$SU(2)_{L,12} \times SU(2)_{L,3}$	$O_{qq}^{(3)}, O_{lq}^{(3)}$	$O_{lq}^{(3)}$ (ll and lv)	$O_{Hq}^{(3)}, O_{Hl}^{(3)}$
$U(1)_{Y,12} \times U(1)_{Y,3}$	$O_{qq}^{(1)}, O_{dd} \dots, O_{lq}^{(1)}, O_{qe}, \dots$	$O_{lq}^{(1)}, O_{qe}, O_{eu}, O_{ed}, \dots$	$O_{Hq}^{(1)}, O_{Hl}^{(1)}, O_{He}, \dots, O_{HD}$

⇒ **Complementary constraints** from (i) flavour observables, (ii) colliders i.e. LHC, (iii) EW precision

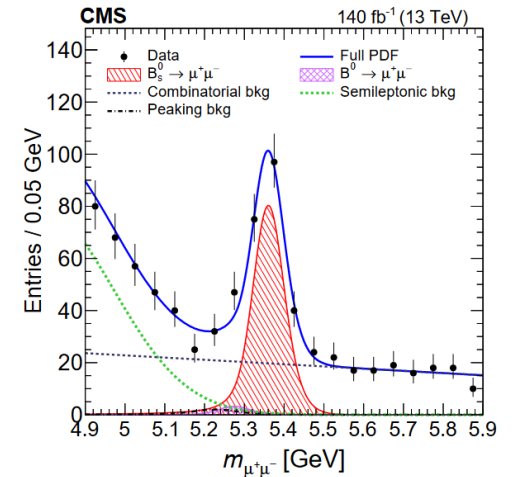
Flavour, key observable is the rare decay $BR(B_s \rightarrow \mu^+ \mu^-)$, measured precisely at LHC

- Weaker bounds for $DU(1)_Y$ because $Y_Q g_Y \sim 1/18$ vs $t_L^3 g_L \sim 1/3$

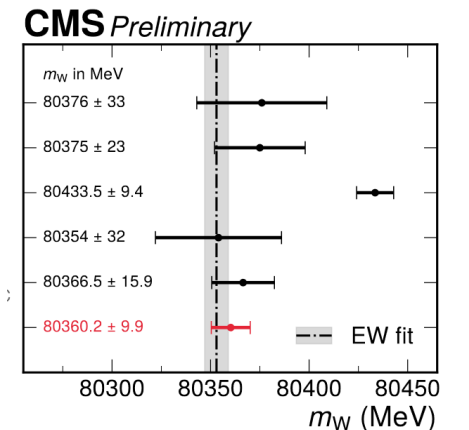
LHC Drell-Yan driven by valence-quark couplings: bounds favour $g_3 \gg g_{12}$ region i.e. $\theta \rightarrow \pi/2$

EWPOs: tree-level shifts in Z -pole observables & m_W means EW constraints often strongest!

- Key observable given current data is W mass: $DSU(2)_L$ gives $\delta m_W < 0$; $DU(1)_Y$ gives $\delta m_W > 0$



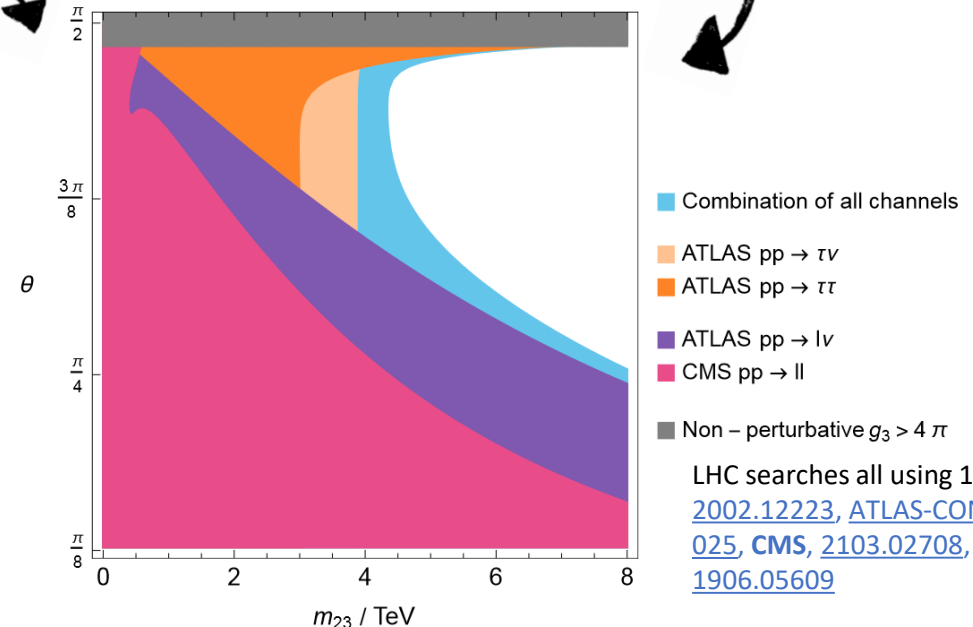
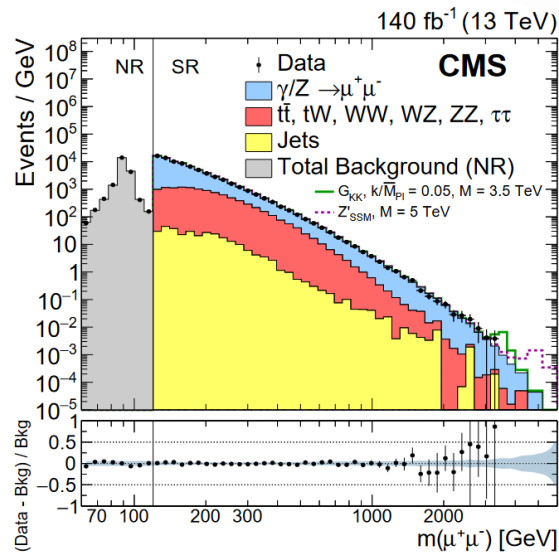
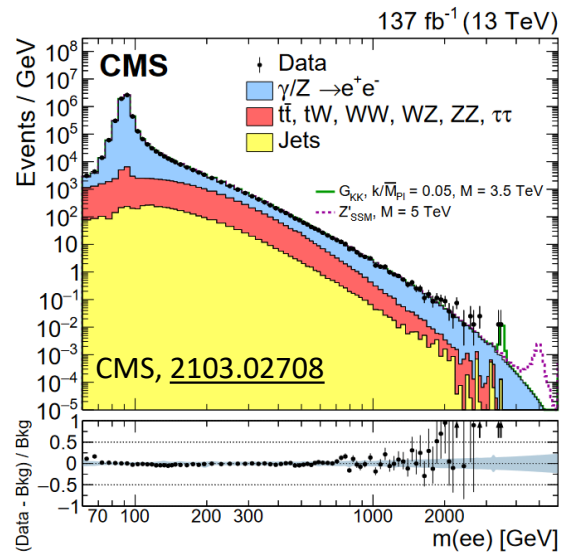
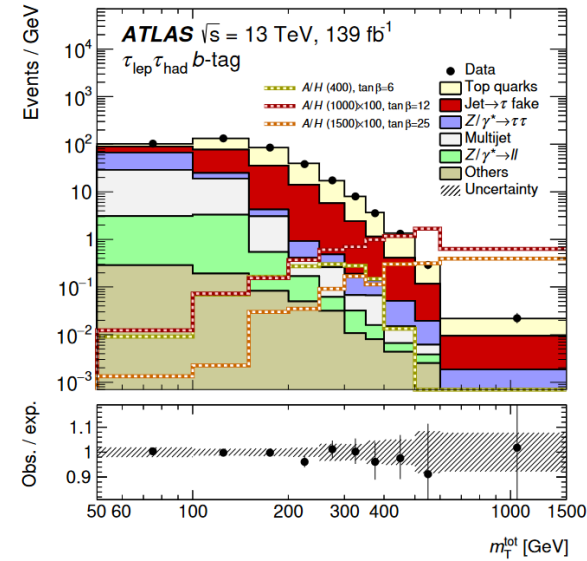
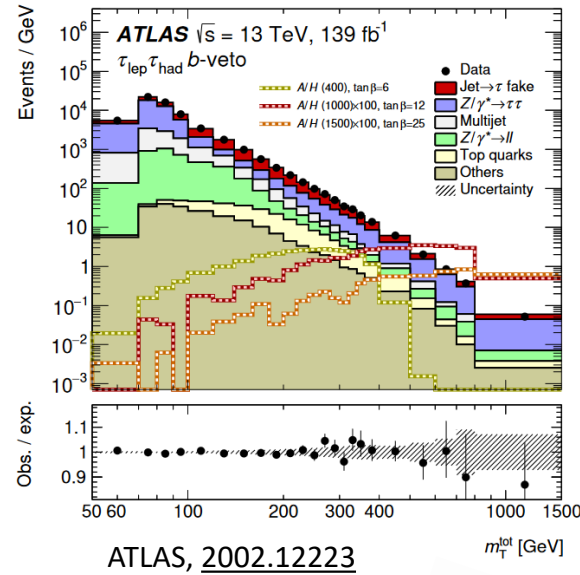
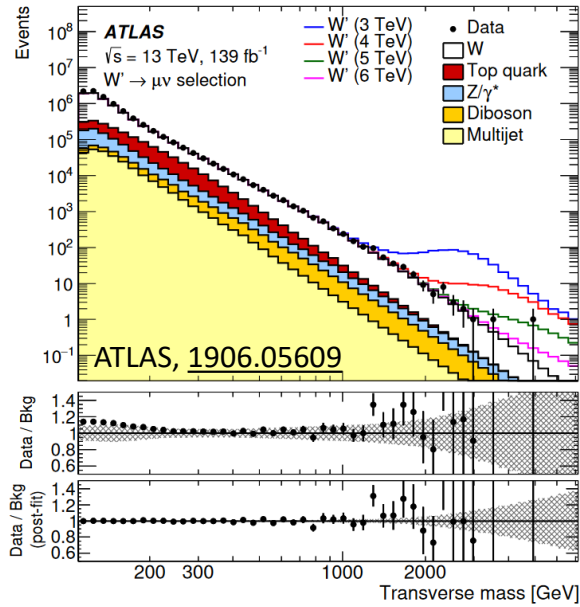
CMS, [2212.10311](#)



CMS, [2024](#)

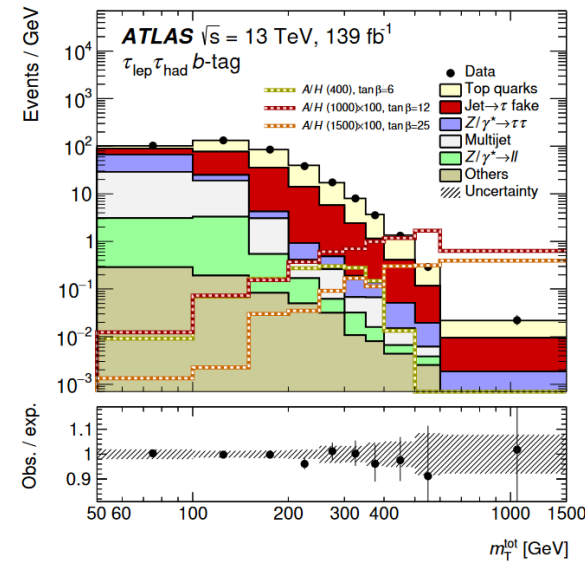
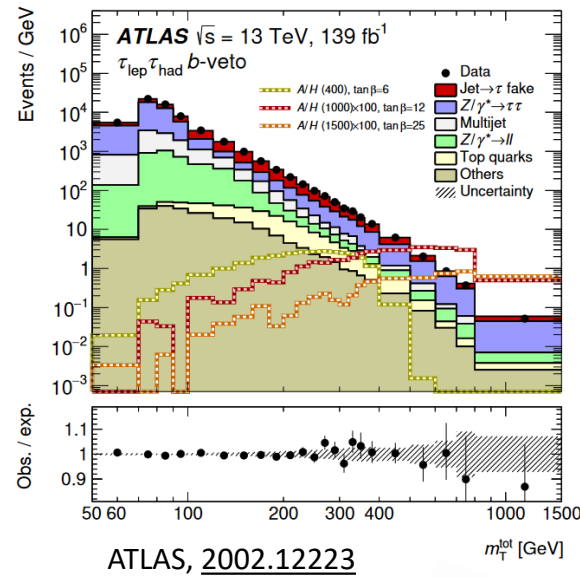
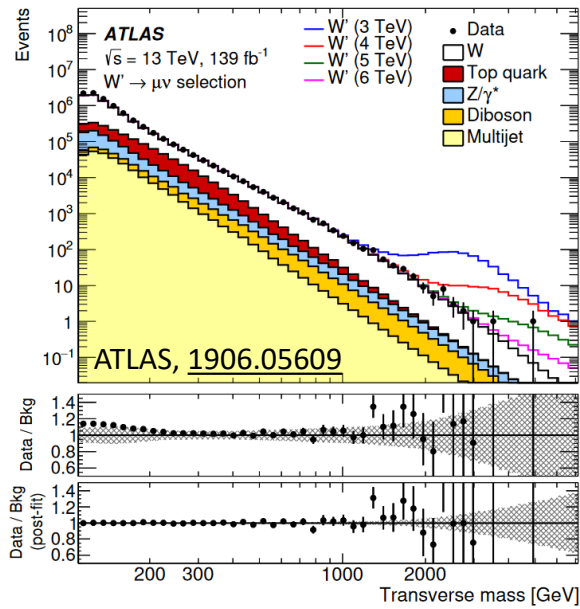
[Sadly not included in our fits yet...]

Hight pT LHC constraints



LHC searches all using 139 fb^{-1} :
[2002.12223](#), [ATLAS-CONF-2021-025](#), [CMS, 2103.02708](#), [ATLAS, 1906.05609](#)

Hight pT LHC constraints

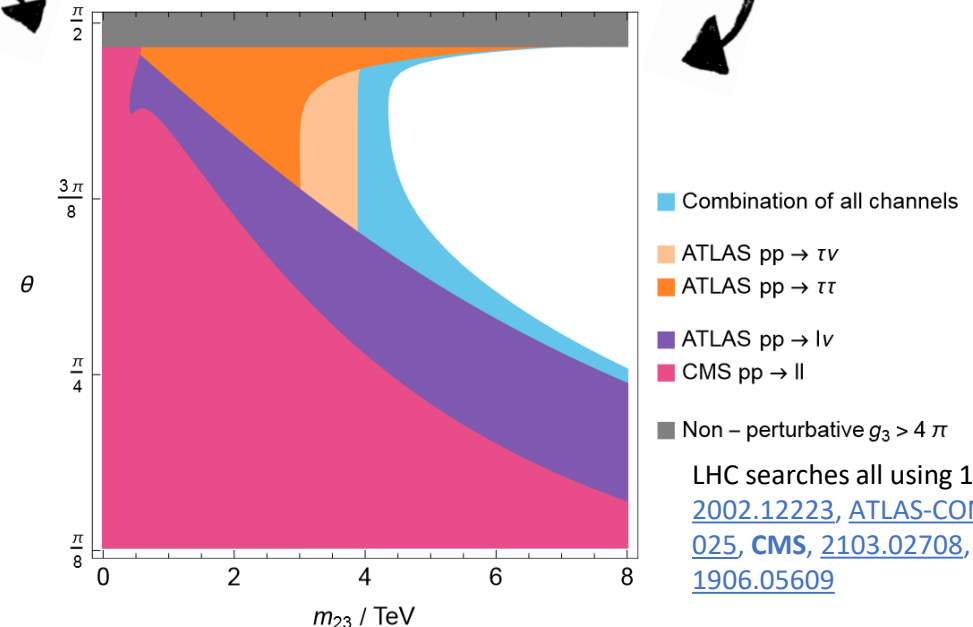
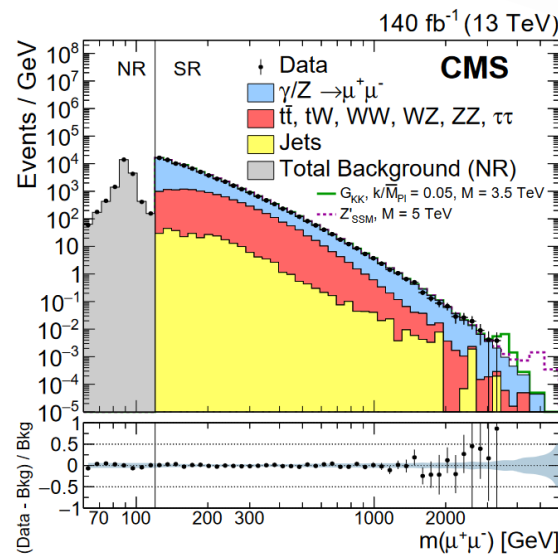
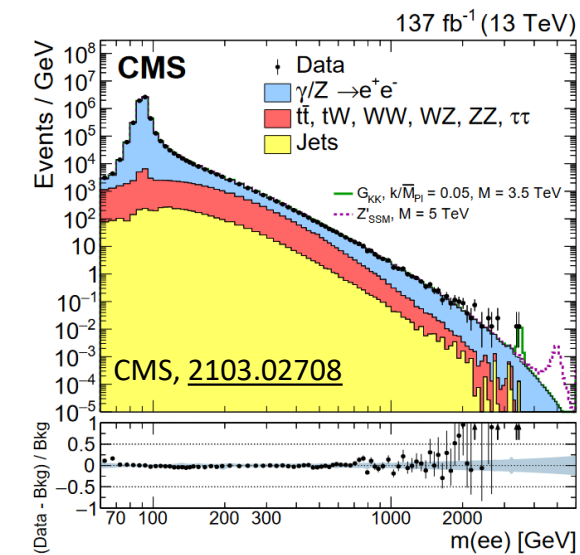


So far we just used LHC Drell-Yan data to constrain the models

Many other collider probes are possible!

- $X \rightarrow HZ \rightarrow \dots$
- $X \rightarrow Z\phi \rightarrow (\mu\mu)(HH) \rightarrow \dots$

[in brainstorming phase...]



LHC searches all using 139 fb⁻¹:
[2002.12223](#), [ATLAS-CONF-2021-025](#), [CMS, 2103.02708](#), [ATLAS, 1906.05609](#)

High p_T LHC constraints

Stronger constraints on the 3rd family aligned $SU(2)_L$ likely already exist! To be explored...

[ATLAS, 2402.10607](#)

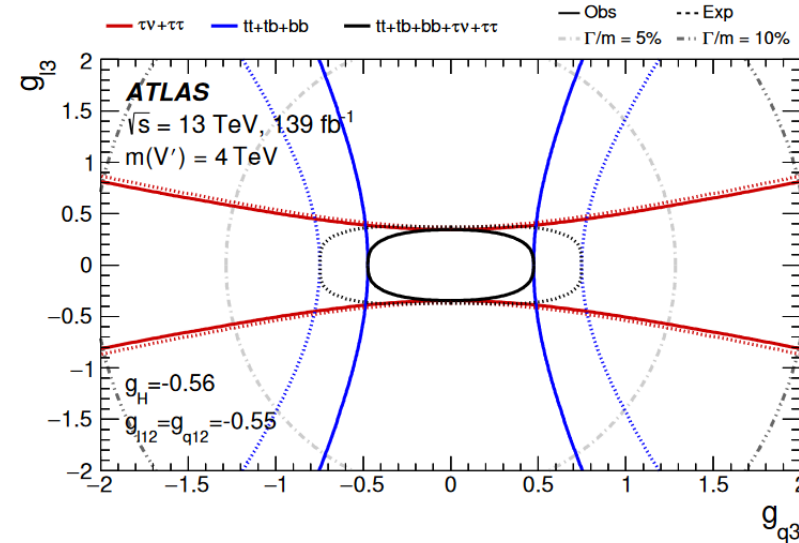
Combination of searches for heavy spin-1 resonances using 139 fb^{-1} of proton-proton collision data at $\sqrt{s} = 13 \text{ TeV}$ with the ATLAS detector

The ATLAS collaboration

E-mail: atlas.publications@cern.ch

ABSTRACT: A combination of searches for new heavy spin-1 resonances decaying into different pairings of W , Z , or Higgs bosons, as well as directly into leptons or quarks, is presented. The data sample used corresponds to 139 fb^{-1} of proton-proton collisions at $\sqrt{s} = 13 \text{ TeV}$ collected during 2015–2018 with the ATLAS detector at the CERN Large Hadron Collider.

Analyses selecting quark pairs (qq , bb , $t\bar{t}$, and $t\bar{b}$) or third-generation leptons ($\tau\nu$ and $\tau\tau$) are included in this kind of combination for the first time. A simplified model predicting a spin-1 heavy vector-boson triplet is used. Cross-section limits are set at the 95% confidence level and are compared with predictions for the benchmark model. These limits are also expressed in terms of constraints on couplings of the heavy vector-boson triplet to quarks, leptons, and the Higgs boson. The complementarity of the various analyses increases the sensitivity to new physics, and the resulting constraints are stronger than those from any individual analysis considered. The data exclude a heavy vector-boson triplet with mass below 5.8 TeV in a weakly coupled scenario, below 4.4 TeV in a strongly coupled scenario, and up to 1.5 TeV in the case of production via vector-boson fusion.



Does not directly map onto deconstruction model

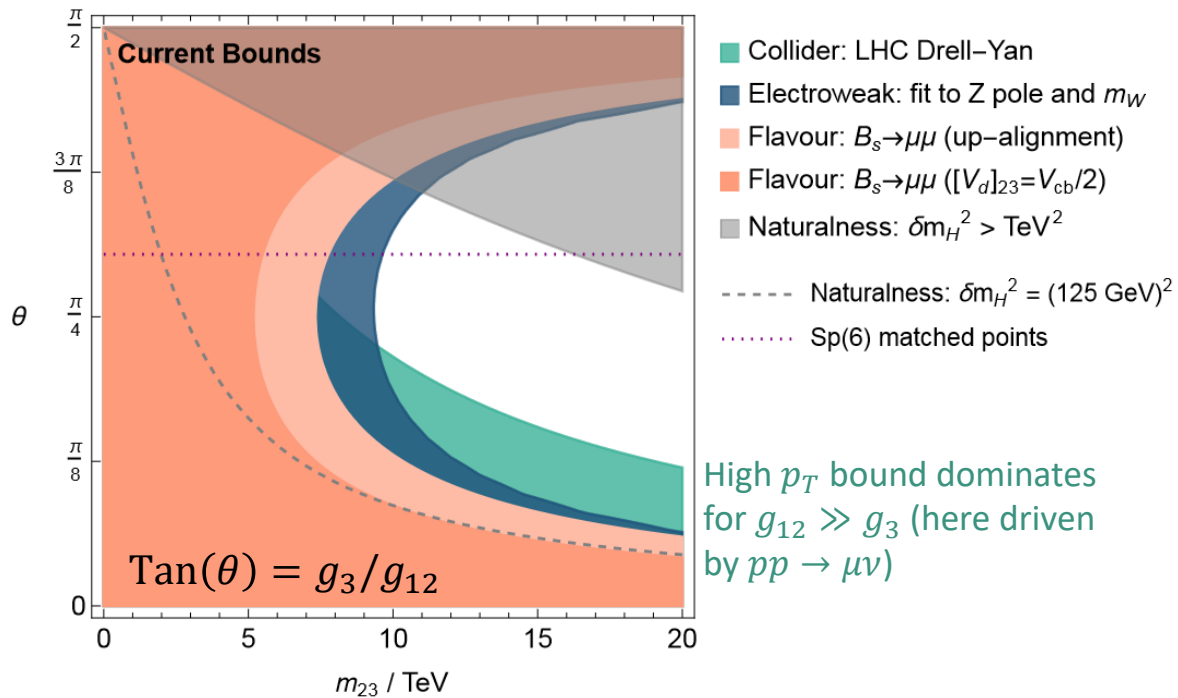
[Assumes Higgs coupling tied to light generations, not third, and assumes fixed light family couplings]

In similar ballpark to the 4-5 TeV exclusion we estimated from Drell-Yan, but looks stronger

Deconstructed $SU(2)_L$ summary

Davighi, Gosnay, Miller, Renner [2312.13346](#)

See also Capdevila, Crivellin, Lizana, Pokorski [2401.00848](#)



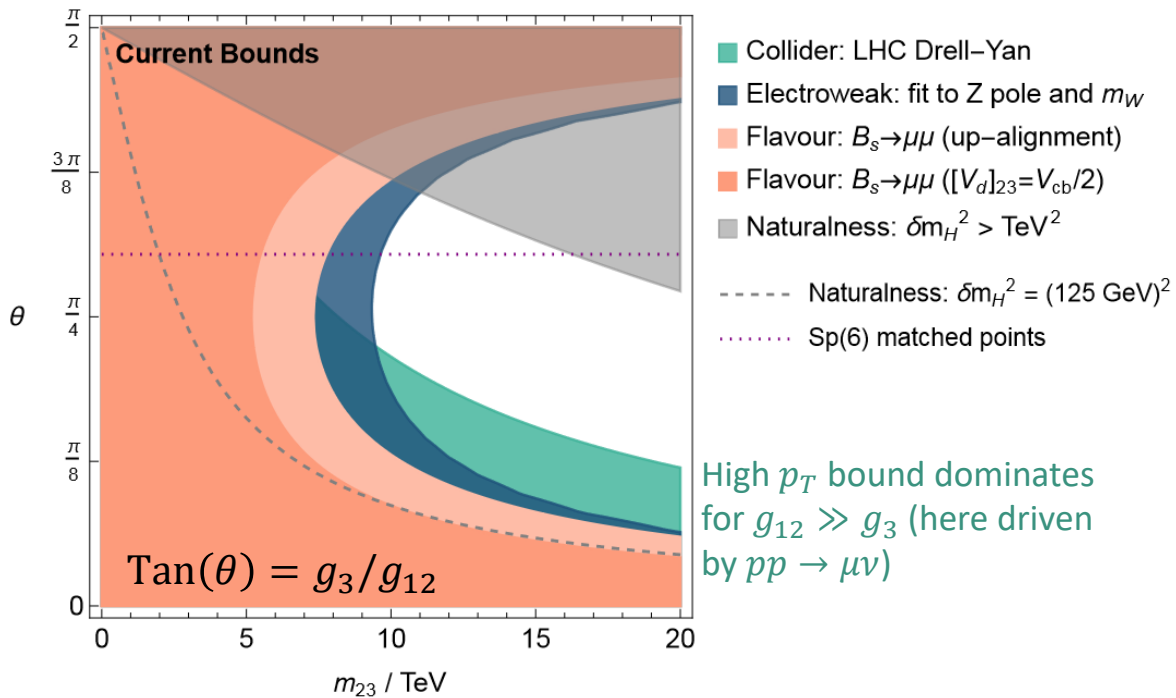
Current: $M_{W'_L, Z'_L} > 9 \text{ TeV}$

Driven by EWPOs; flavour and LHC complementary
Plenty of **natural parameter space remains!**

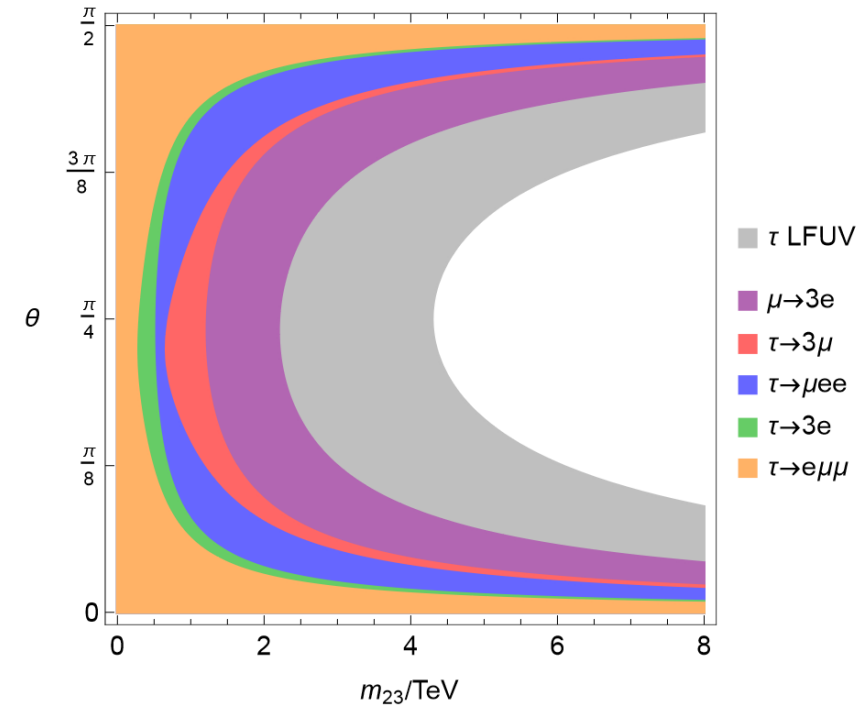
Deconstructed $SU(2)_L$ summary

Davighi, Gosnay, Miller, Renner [2312.13346](#)

See also Capdevila, Crivellin, Lizana, Pokorski [2401.00848](#)



What about Leptons?



- LFUV (tau vs e/mu) is predicted by the model
- LFV not predicted, but can naturally be CKM-like

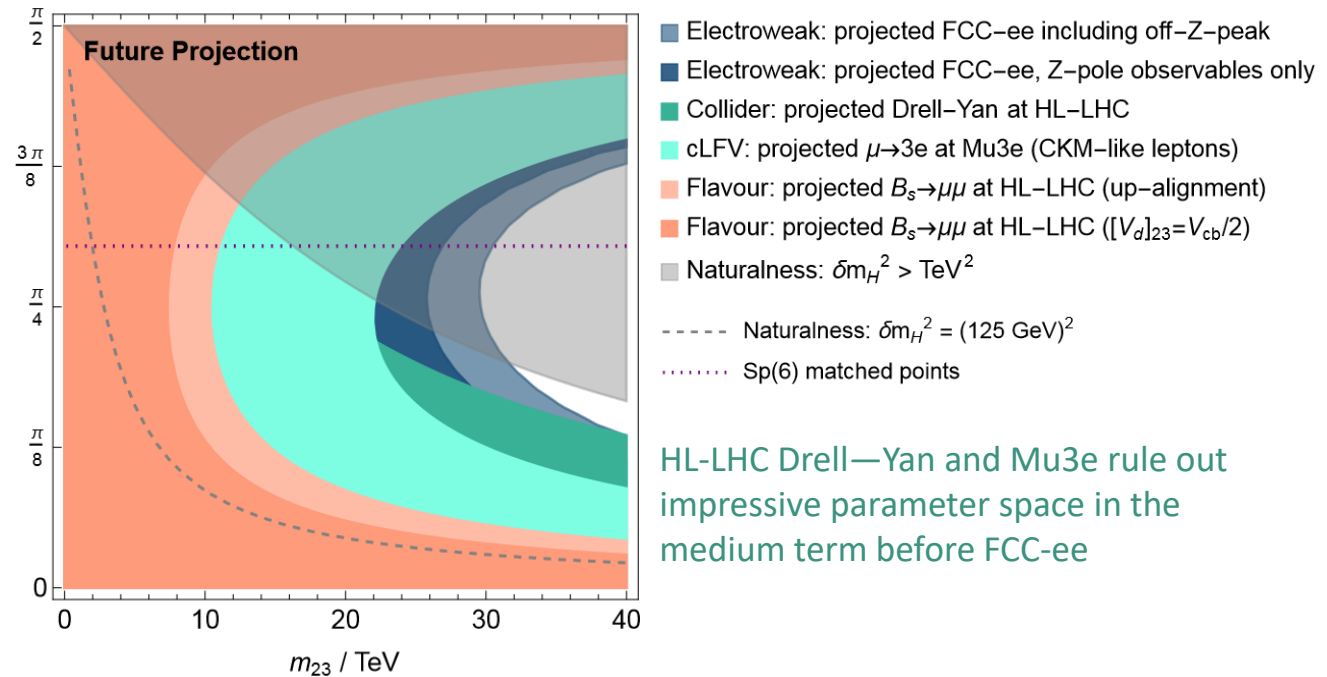
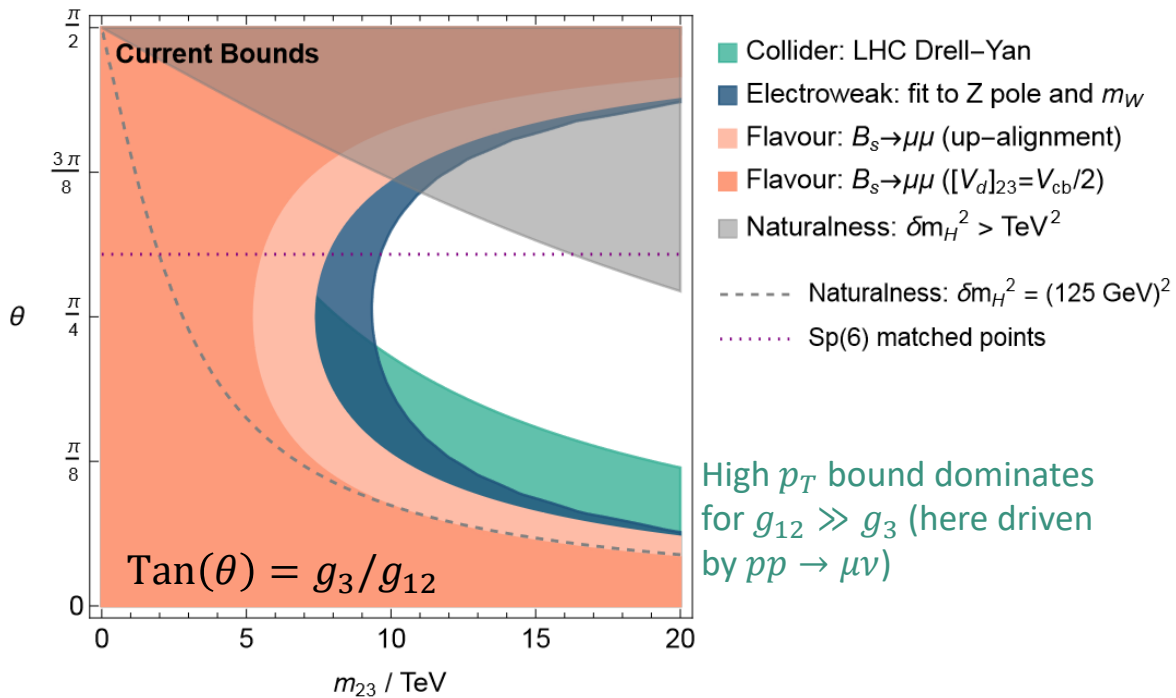
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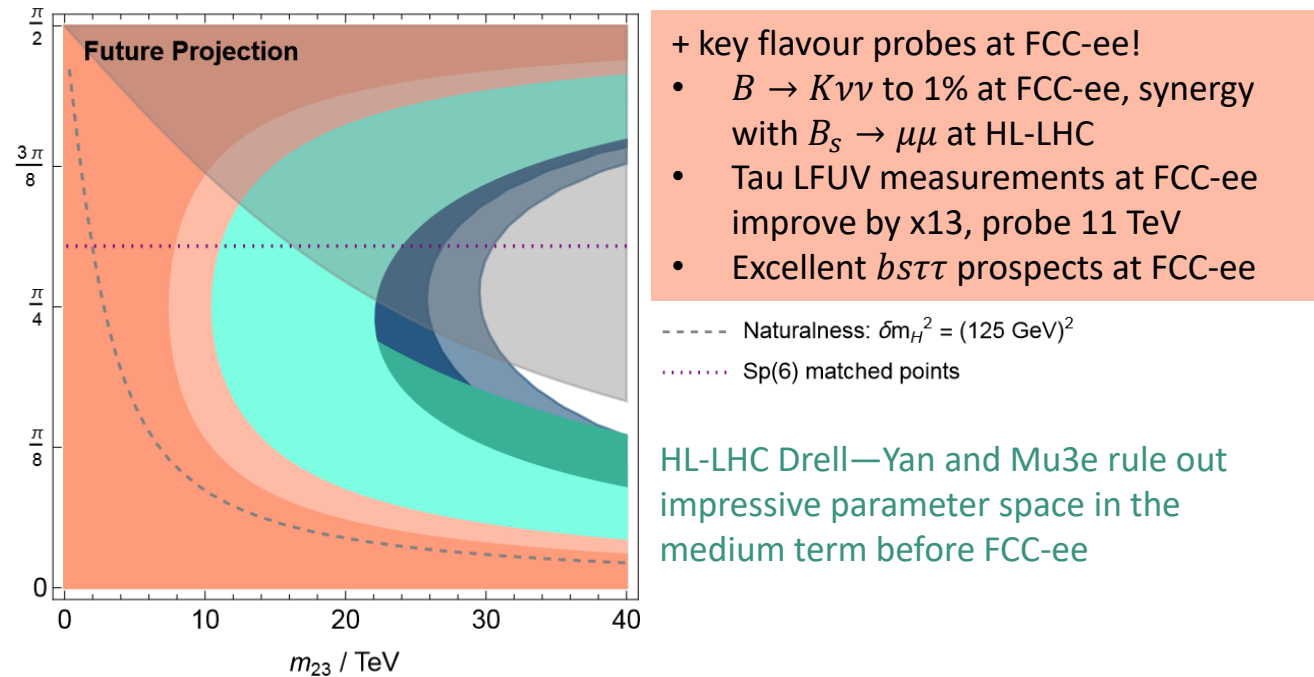
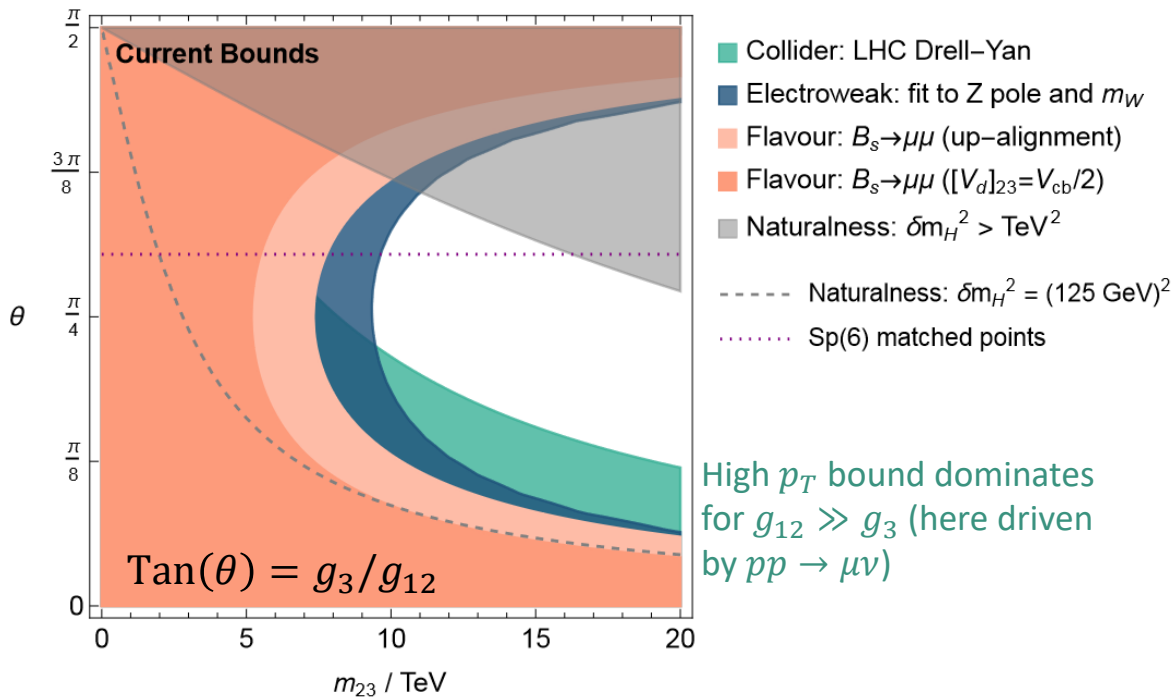
FCC-ee: $M_{W'_L, Z'_L} > 30 \text{ TeV}$

A tera-Z EW precision programme can cover entire
natural parameter space

Deconstructed $SU(2)_L$ summary

Davighi, Gosnay, Miller, Renner [2312.13346](#)

See also Capdevila, Crivellin, Lizana, Pokorski [2401.00848](#)



- + key flavour probes at FCC-ee!
- $B \rightarrow K\nu\nu$ to 1% at FCC-ee, synergy with $B_s \rightarrow \mu\mu$ at HL-LHC
- Tau LFUV measurements at FCC-ee improve by x13, probe 11 TeV
- Excellent $b s \tau \tau$ prospects at FCC-ee

Current: $M_{W'_L, Z'_L} > 9 \text{ TeV}$

Driven by EWPOs; flavour and LHC complementary
Plenty of **natural parameter space remains!**

FCC-ee: $M_{W'_L, Z'_L} > 30 \text{ TeV}$

A tera-Z EW precision programme can cover entire
natural parameter space

Deconstructed $U(1)_Y$

Davighi, Stefaneke [2305.16280](#)

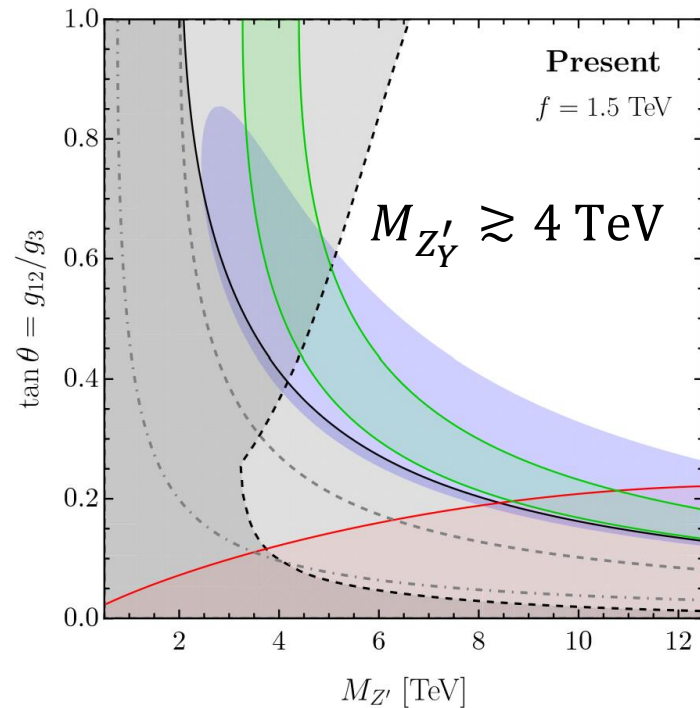
See also
 Fernández Navarro, King [2305.07690](#)
 Allanach, Davighi [1809.01158](#)

More natural model; double benefit from $g_Y \sim g_L/2$ (roughly x2 smaller δm_h^2 , roughly x2 smaller NP effects)

	Flavour (mixing, $bs\mu\mu$)	LHC Drell-Yan $pp \rightarrow ll$	Electroweak Precision
$U(1)_{Y,12} \times U(1)_{Y,3}$	$O_{qq}^{(1)}, O_{dd} \dots, O_{lq}^{(1)}, O_{qe}, \dots$	$O_{lq}^{(1)}, O_{qe}, O_{eu}, O_{ed}, \dots$	$O_{Hq}^{(1)}, O_{Hl}^{(1)}, O_{He}, \dots, O_{HD}$

LL 4-quark operators especially small thanks to $Y_Q g_Y \sim 1/18$

+ve shift in M_W currently preferred by EW fit (even ignoring CDF II measurement)



- B_s mixing (with up-alignment! Suppressed by $Y_Q g_Y$)
- $B_s \rightarrow \mu\mu$ exclusion (strong-ish because our $bs\mu\mu$ is $\approx C_{10}$)
- Electroweak fit (1 sigma) using a new M_W average
- Electroweak fit (2 sigma exclusion) excluding CDF II M_W
- High p_T exclusion (recast of $pp \rightarrow ee, \mu\mu, \tau\tau$ searches)
- Percent tuning in M_h^2
- A "natural" explanation of fermion mass hierarchies

Phenomenology of EW Flavour Deconstruction

Summary:

	Deconstructed $SU(2)_L$	Deconstructed $U(1)_Y$
Electroweak: Z-pole & W-pole	9 TeV (5 TeV if exc. m_W)	2 TeV
Flavour: $B_s \rightarrow \mu\mu$ (up-alignment)	7.5 TeV	2 TeV
High p_T : Drell–Yan $pp \rightarrow ee, \mu\mu, \tau\tau$	4.5 TeV	3.5 TeV
EW projection FCC-ee: on and off Z-pole & W-pole	30 TeV	7 TeV

[Davighi, Gosnay, Miller, Renner 2312.13346](#)

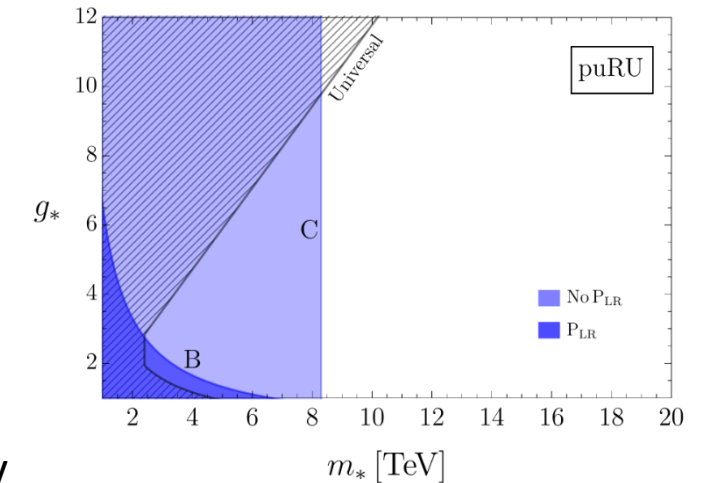
[Davighi, Stefanek 2305.16280](#)

4. Deconstructing the Composite Higgs

Covone, Davighi, Isidori, Pesut, [2407.10950](#)

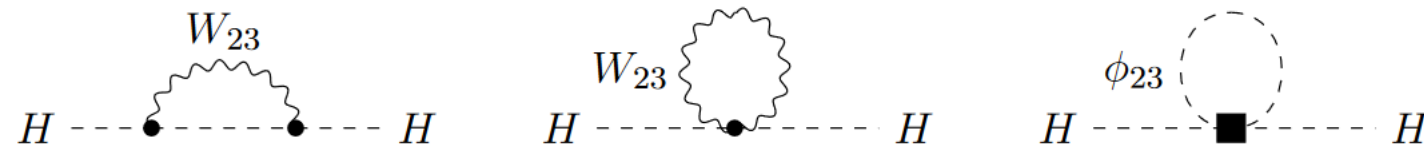
Back to the Hierarchy Problem

We earlier saw that U2 flavour symmetry is needed for a low-scale ($1 \div 2$ TeV) composite Higgs solution to hierarchy problem



We also saw that flavour deconstruction can solve the flavour puzzle near the TeV

- BUT that electroweak precision tests (+ flavour + high pT) are pushing us to regions with large finite δm_h^2
- Motivates us to solve the hierarchy problem simultaneously



→ **joint solution** near TeV of hierarchy problem & flavour puzzle?

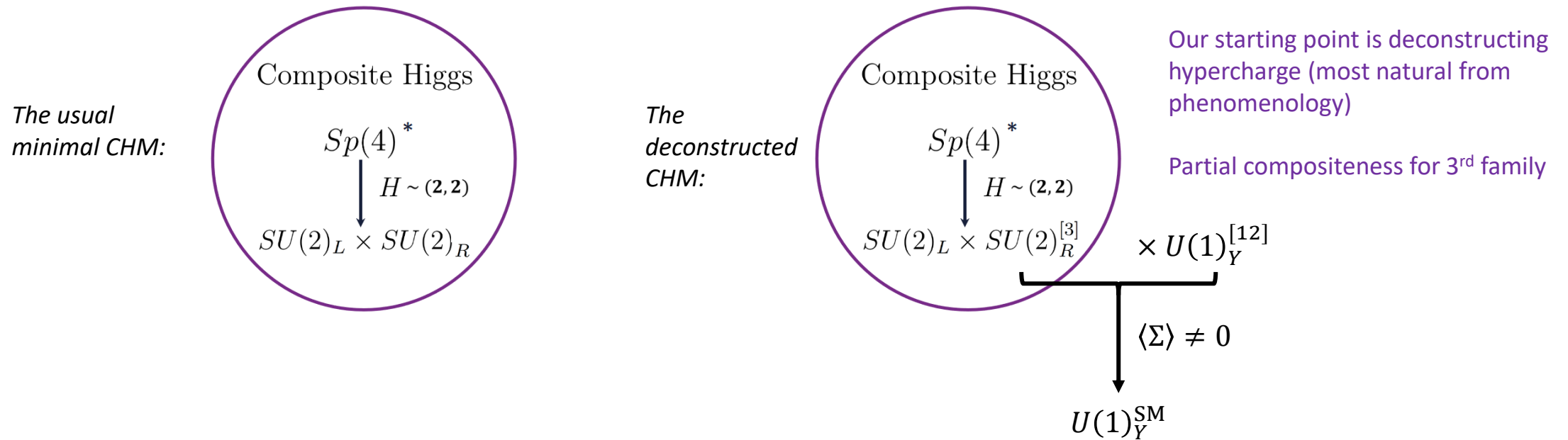
Maybe the flavour deconstruction can even help *reduce* the little hierarchy in a composite Higgs model?

Flavour Deconstructing the Composite Higgs

Covone, Davighi, Isidori, Pesut, [2407.10950](#)

Flavour deconstructed gauge interactions can be elegantly combined with a composite Higgs

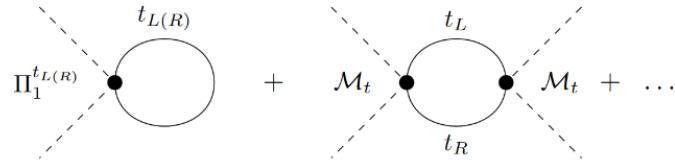
Recap: a light composite Higgs = pNGB from global symmetry breaking in a BSM strong sector (like QCD pions)



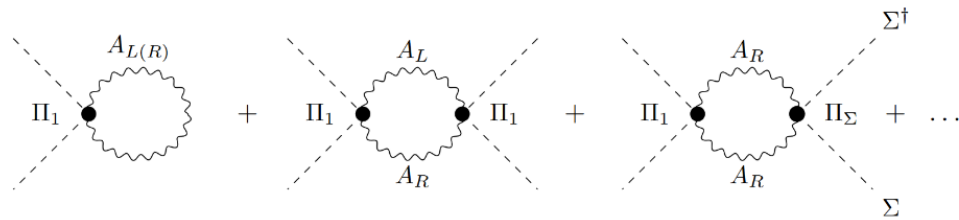
- **BSM flavour puzzle:** delivers **gauge explanation** for the $U(2)$ protection that we saw can lower compositeness scale!
- Explains the **SM flavour puzzle** in the same dynamical step(s)!

Deconstructing the composite Higgs potential

The Higgs potential is generated at one-loop by top Yukawa and gauging the (deconstructed) EW symmetry:



Fermion (top)
contributions,
cut off by M_T

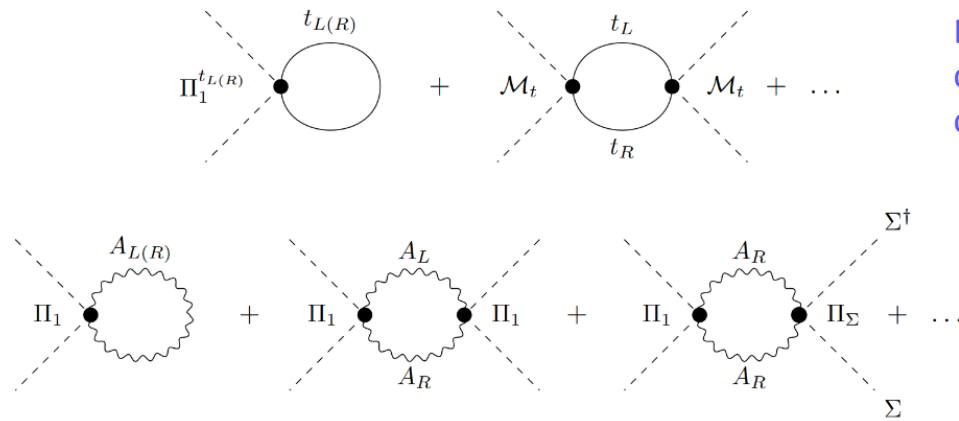


EW gauge
boson
contributions,
cut off by M_ρ

$$\rightarrow m_h^2 = \frac{1}{16\pi^2} \left[4n_c y_t^2 M_T^2 - \frac{9}{2} g_{R,3}^2 M_\rho^2 \left(1 - \frac{2M_{W_R}^2}{M_\rho^2} \right) \right]$$

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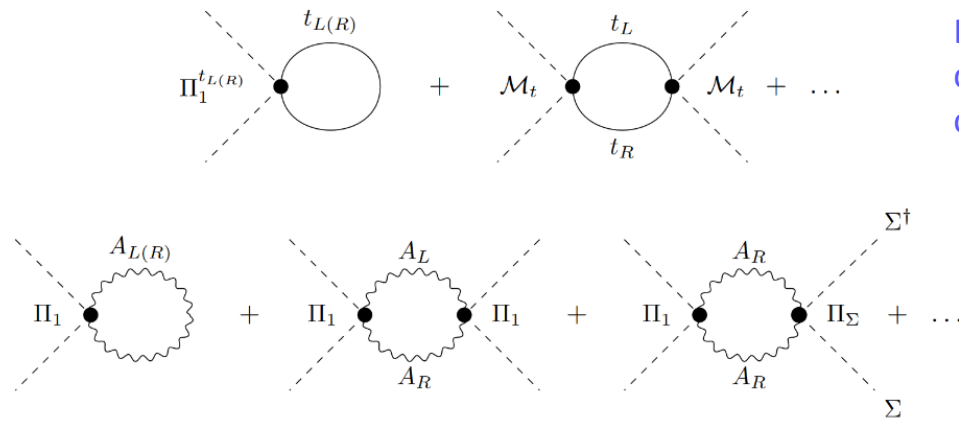
In addition to solving the SM + BSM flavour puzzles, deconstructing the CH brings further benefits:

Deconstruction helps the CHM be more natural!

- Gauge coupling $g_{R,3}^2$ can be pumped up w.r.t SM g_Y to better cancel top Yukawa contribution to m_h^2
- Numerically, this allows top partner to be heavier ($M_T > 1.5$ TeV), better compatibility with direct searches

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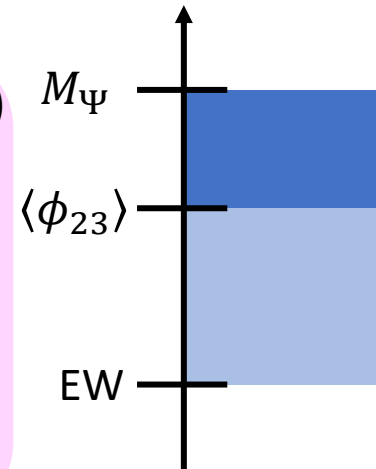
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CH makes deconstruction more predictive! (+ natural)

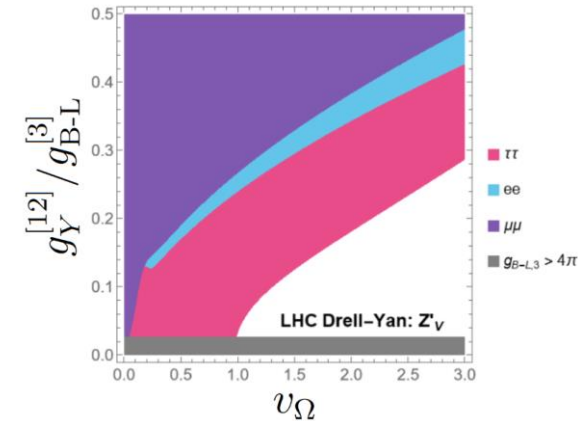
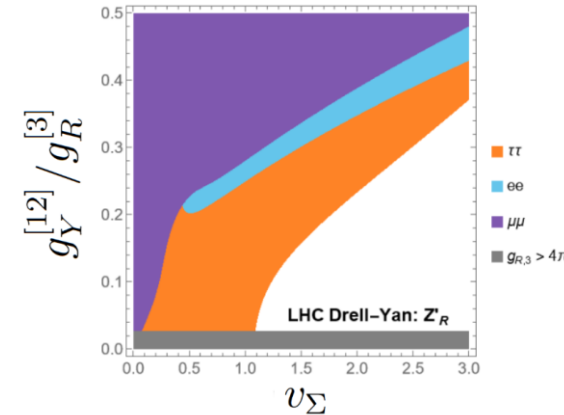
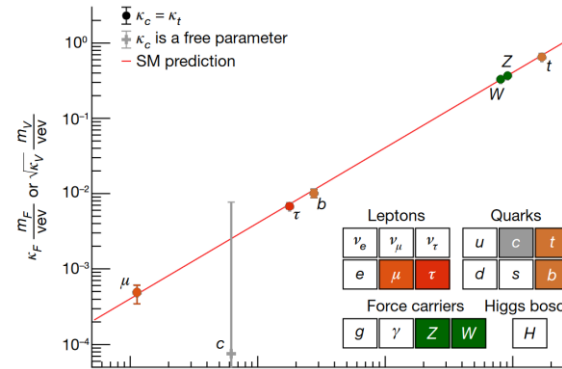
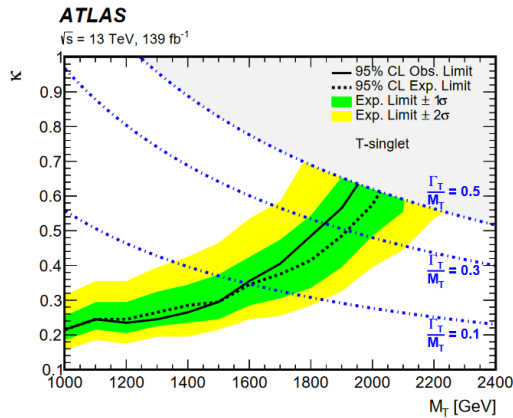
- Require $2M_{W_R}^2 < M_\rho^2$ to avoid sign flip in m_h^2 , i.e. deconstruction bosons must be sufficiently light
- Experiment dictates $M_{W_R} > \text{few TeV}$. Squeezed!
- To explain $y_2 \ll y_3$, need $M_\Psi > \text{few 100 TeV}$. Now this gives no radiative contribution to Higgs mass thanks to compositeness at lower scale ☺



Sketching the Phenomenology

The pheno of this complicated model resembles that of minimal CHM with U2 *SMASH* deconstructed gauge bosons

- Modified HWW and HZZ couplings
- Top partners and higher composite resonances
- Universal shifts in EWPOs
- Flavour constraints e.g. $B \rightarrow X_s \gamma$ particularly strong
- LHC Drell–Yan bounds on heavy gauge bosons
- Extra shifts in EWPOs



We didn't do a full pheno study of this model, but the following benchmark scenario is viable:

- Large $g_{R,3} \sim 1$
- Light top partner $M_T \approx 2 \text{ TeV}$; spin-1 resonance $M_\rho \approx 10 \text{ TeV}$
- Deconstruction scale $v_\Sigma \approx 3 \text{ TeV}$
- Order 5% tuning in Higgs mass

Conclusions

1. The Higgs remains a central motivation for high-energy BSM. Flavour cannot be overlooked.
2. From MFV to U2 flavour symmetries can realise lower Λ_{NP} : more natural BSM solutions to hierarchy problem (or any other problem/puzzle...)
3. U2-like models have the ingredients to also **solve the flavour puzzle** at low-scale: hypothesis of **flavour non-universal gauge interactions** e.g. flavour deconstruction
4. Rich phenomenology across quark and lepton flavour, EWPOs, high pT measurements at LHC
5. Fruitful to pursue flavour non-universal models that solve flavour puzzle **and** hierarchy problem simultaneously, e.g. deconstructed CH, even if they appear complicated...

Thank you!

Backup

How to generate flavour in Composite Higgs Models?

The problem with elementary fermions: $L_{\text{strong}} \supset \frac{1}{\Lambda^{d-1}} \bar{q} O_H u + \Lambda^{4-d'} O_H O_H^\dagger + \frac{1}{\Lambda^2} (\bar{q} q)^2$ Cannot have Λ low due to flavour bounds

O_H is a composite scalar operator with quantum numbers of Higgs.
Want $d \approx 1$ to get large top Yukawa

Want $O_H O_H^\dagger$ to be irrelevant!
But $d \approx 1$ (quasi-free) implies $d' \approx 2d \approx 2$

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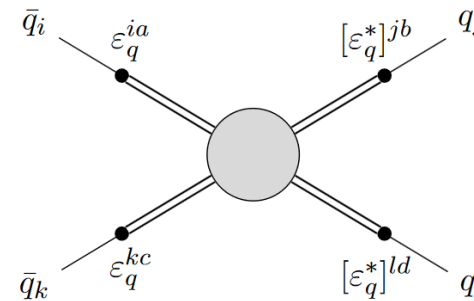
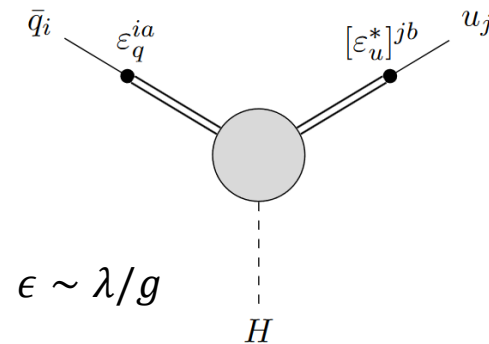
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Partial Compositeness is a solution: $L \supset \lambda_q^{ia} \bar{q}_i O_a^q + \lambda_u^{ia} \bar{u}_i O_a^u + \bar{O}_a^q O_H O_b^u$

Kaplan, [1991](#)
Review: Panico, Wulzer, [1506.01961](#)



Yukawa couplings now generated by **relevant** operators

Aside: Flavour from Anarchy?



Partial compositeness even promised a *dynamical solution* to *flavour puzzle*:

- The $\lambda_q^{ia} \bar{q}_i O_a^q$ mixing operators run with scale
- If λ_q^{ia} anarchic at high scale Λ_{high} , slight differences in anomalous dimensions of O_a^q transmute to *exponential hierarchies* in the resulting “proto-Yukawas” at scale m_*

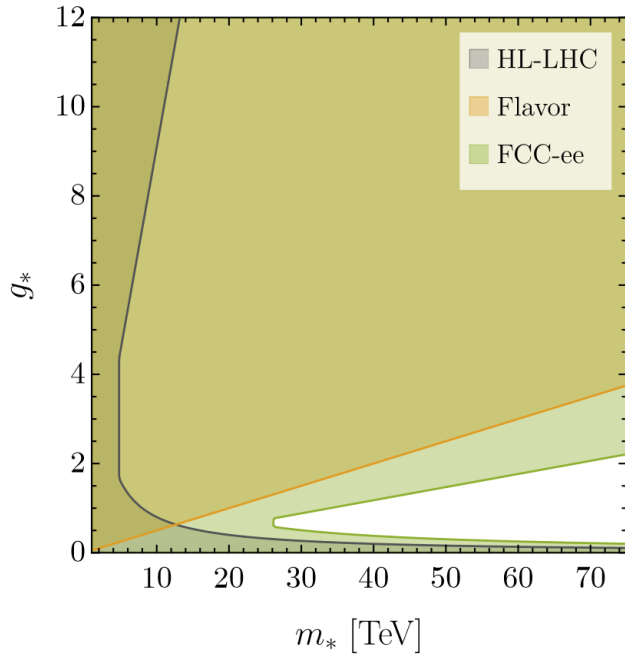
$$\lambda_\psi^{ia}(m_*) \simeq \lambda_\psi^{ia}(\Lambda) \left(\frac{m_*}{\Lambda}\right)^{\gamma_\psi^a} \equiv \lambda_\psi^{ia}(\Lambda) e^{-\gamma_\psi^a L}, \quad L \equiv \ln \Lambda/m_*$$

- BUT this entails large flavour violation also at m_*
- Strongest bound from neutron EDM $\Rightarrow M_* \gtrsim 20 \div 25 \text{ TeV}$
[Even assuming 1-loop suppressed quark dipole operators]
- Such a high scale degrades this as a solution to the hierarchy problem AND is untestable in colliders
- We **need** a flavour symmetry to bring down m_* . Let’s compare MFV vs. $U(2)$ -like

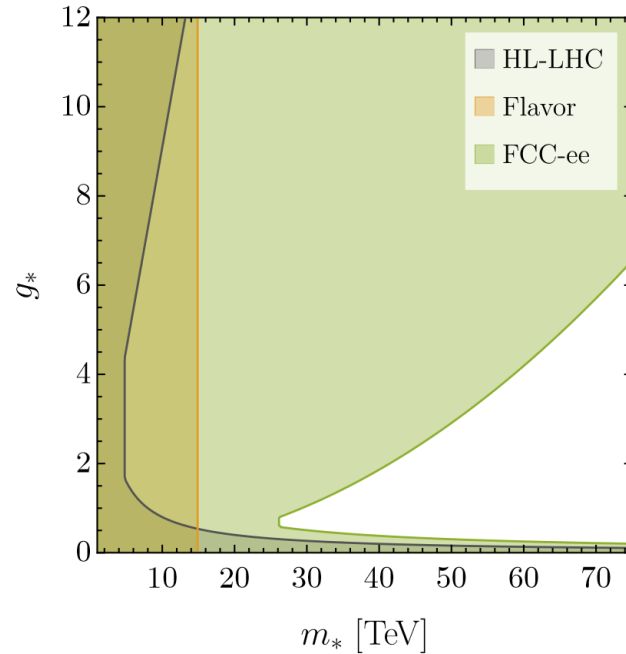
Future Prospects: HL-LHC, FCC-ee

Stefanek, [2407.09593](#)

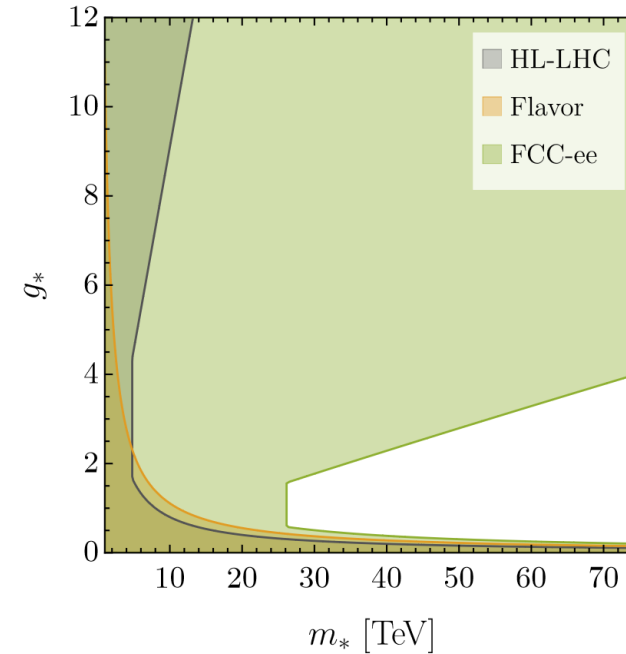
- FCC-ee “tera-Z” run: approx. 10^5 times LEP dataset on Z-pole
- With this precision, RG-running into EWPOs at 1-loop (and even 2-loop) is crucially important



(a) Left compositeness



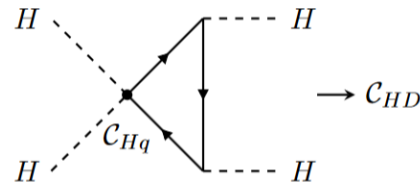
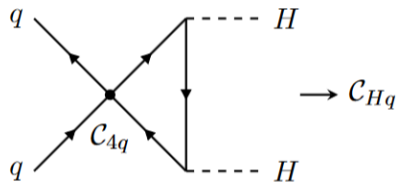
(b) Mixed compositeness



(c) Right compositeness

All 3 scenarios have $U(2)_{u_R} \times U(2)_{q_L}$

- All sectors contribute to EWPO bounds at this precision, including e.g. 4 top operators which shift m_W at NLL



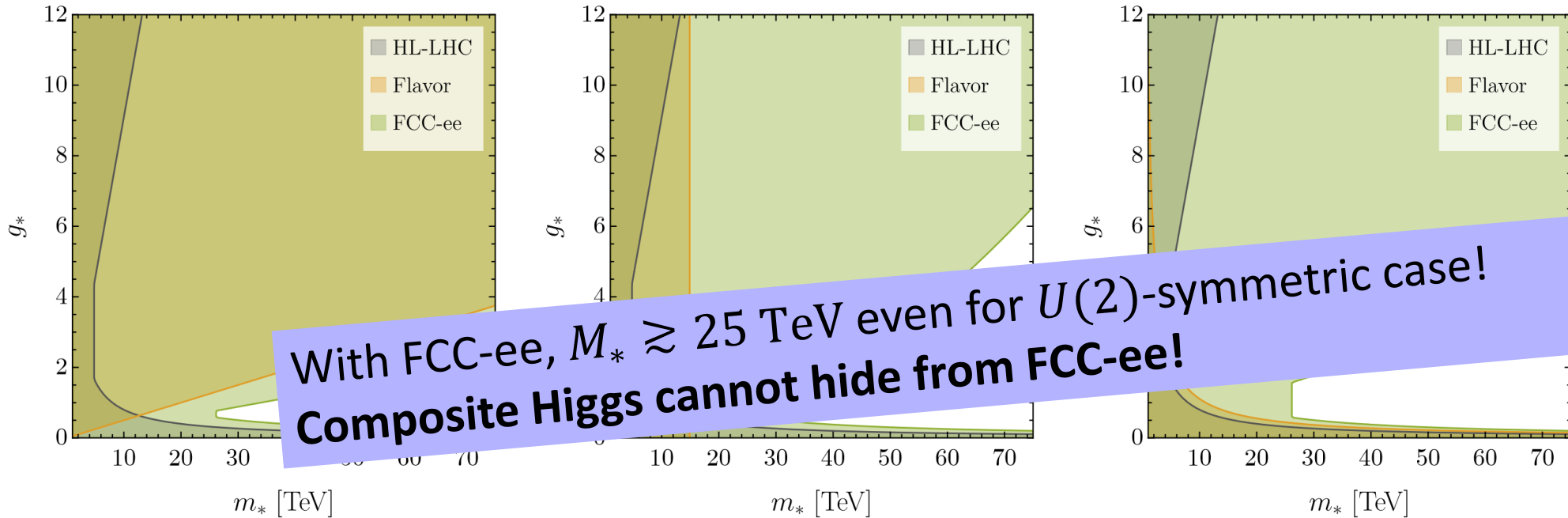
Even current EWPOs give stronger constraint on $O_{tt} \sim (t\bar{t})^2$ than LHC $pp \rightarrow t\bar{t}$ and $pp \rightarrow t\bar{t}t\bar{t}$ measurements!

c.f. also Allwicher et al, [2302.11584](#)

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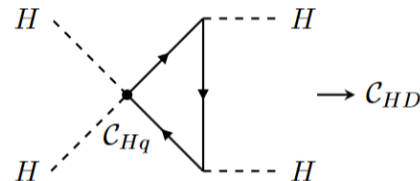
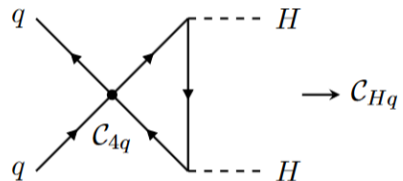


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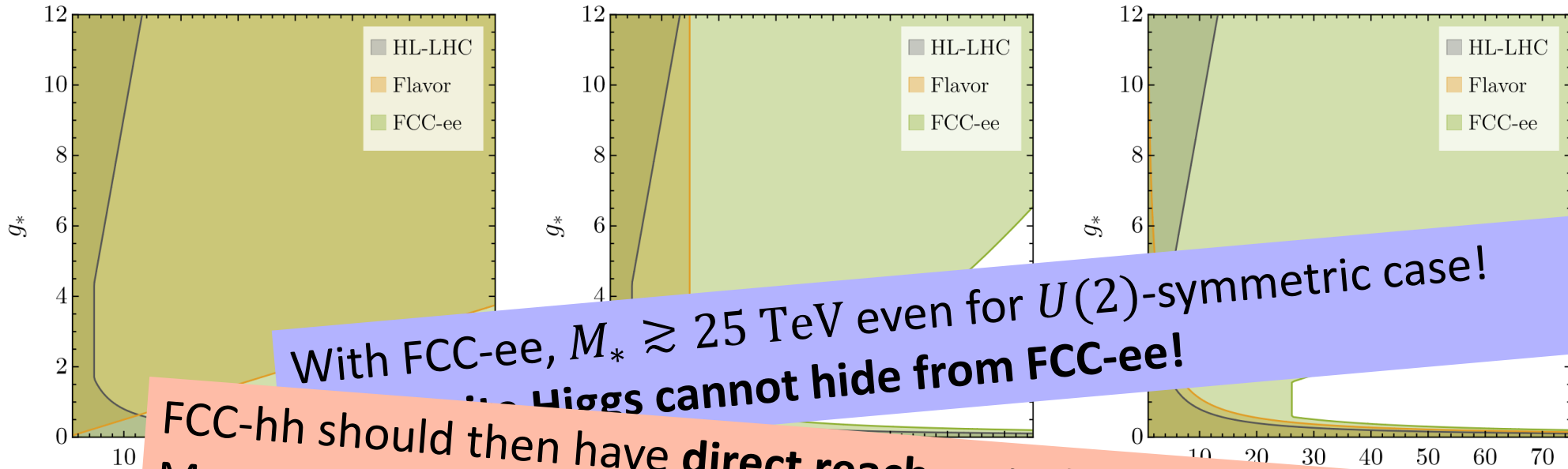


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With FCC-ee, $M_* \gtrsim 25$ TeV even for $U(2)$ -symmetric case!

... Higgs cannot hide from FCC-ee!

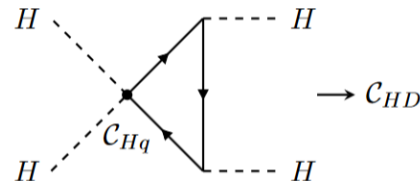
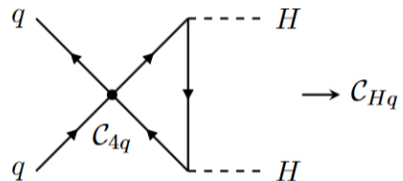
FCC-hh should then have **direct reach** up to $M_* \sim 20$ TeV [Golling et al [1606.00947](#)]

Muon Collider could have direct reach up to $E_{\text{CoM}}/2$ [Accettura et al [2303.08533](#)]

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